

# **Preliminary structural design for Monier Tower**

**Student : Giacomo Butte**

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# 1.Design brief and general assumptions.

## Design brief

Develop a structural design scheme for a 22-storey residential tower. Building to be located in the waterside redevelopment area of a regional city centre.

Building functions.

Level -1	Basement
Level 0,1	Retail area Requirements: 8m column span and 4m height, 2 lifts, one stair core and 2 escalators
Level 2-17	Residential tower. Requirements: one staircase and two lifts.
Level 18	garden area and residential
Level 19-22	penthouse apartments

## Loadings

Given by design brief. These loadings include an allowance for services. All values are characteristic values.

Cladding: precast concrete cladding including glazing	2.0kN/m <sup>2</sup>
Car parking:	2.5 kN/m <sup>2</sup>
Retail:	5.0 kN/m <sup>2</sup>
Residential:	2.5 kN/m <sup>2</sup>
Circulation:	5.0 kN/m <sup>2</sup>
Podium deck:	10.0 kN/m <sup>2</sup>
Garden deck:	10.0 kN/m <sup>2</sup>
Roof:	2.5 kN/m

## Fire safety

The REI120 class required in the design brief may be revised to REI 90 based on Building Code 2010 Approved Document B Table B4.

Based on *BS EN 1992-1-2 Table 5.2a* this would set minimum sizes to:

columns	350mm
distance a	45mm
solid slab	100mm
beams	40mm for 300mm width and 35mm for 400mm width <sup>3</sup> (Table 5.5)

## Durability

Considering a life span of 50 years, exposure class XS1, structural class S4 (in accordance with *EN1992-1-1 Table 4.3N*) the cover required is:

for durability	35mm + 10 mm	<i>EN1992-1-1 Table 4.4N</i>
for bonding (given 20mm rebar)	20mm	
for fire protection	45mm	<i>EN1992-1-2 Table 5.2a</i>

## 2. Wind loads calculation

Basic wind velocity  $v_b := 23.5 \frac{m}{s}$

Dimension of plan parallel to wind  $d := 16m$

Dimension of plan perpendicular to wind  $b := 25m$

Building height  $h := 70.6m$

Terrain roughness for Terrain category 0  
(EN1991-1-4 eq4.5):

$z_0 := 0.003m$   $z_{min} := 1m$   $z_{0.11} := 0.05m$

$$k_r := 0.19 \cdot \left( \frac{z_0}{z_{0.11}} \right)^{0.07} = 0.156$$

$$\text{Roughness factor (EN1991-1-4 eq4.4)} \quad c_r := k_r \cdot \ln \left( \frac{h}{z_0} \right) = 1.571$$

Orographic factor (EN 1991-1-1 4.3.3)  
considered as 1 due to flatness of site:  $c_0 := 1$

Mean wind velocity:  $v_m := c_r \cdot c_0 \cdot v_b = 36.911 \frac{m}{s}$

Wind turbulence (EN1991-1-1-4 eq.4.7)  
k.l considered as 1 as per EN1991-1-1-4 sec4.4(1):

$$k_l := 1 \quad l_v := \frac{k_l}{c_0 \cdot \ln \left( \frac{h}{z_0} \right)} = 0.099$$

Basic velocity pressure (EN1991-1-1-4 sec4.5(1):

$$\rho := 1.25 \frac{kg}{m^3} \quad q_b := \frac{1}{2} \rho \cdot v_b^2 = 0.345 \cdot \frac{kN}{m^2}$$

Peak velocity pressure (EN1991-1-1-4 eq.4.8):

$$q_p := \left( 1 + 7l_v \right) \cdot \frac{1}{2} \rho \cdot v_m^2 = 1.444 \cdot \frac{kN}{m^2}$$

Pressure coefficient type (EN1991-1-4 §7.2.1(1))

External coefficient  $c_{pe}$  defined based on Table 7.1 for the differen zones A,B,C,D,E.

$$c_{peA} := -1.200 \quad c_{peC} := -0.500$$

$$c_{peB} := -0.800 \quad c_{peD} := 0.800 \quad c_{peE} := -0.671$$

Internal pressure coefficients chosen according to EN1991-1-1-4 §7.2.9 as:

$$c_{pi.min} := -0.300 \quad c_{pi.max} := 0.200$$

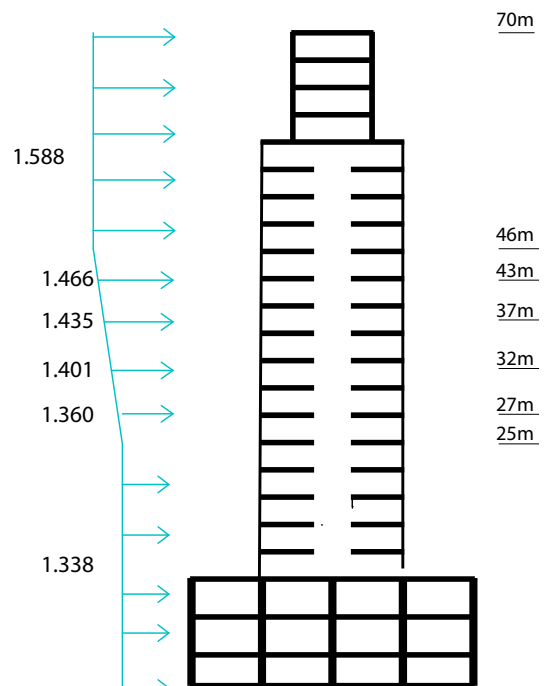
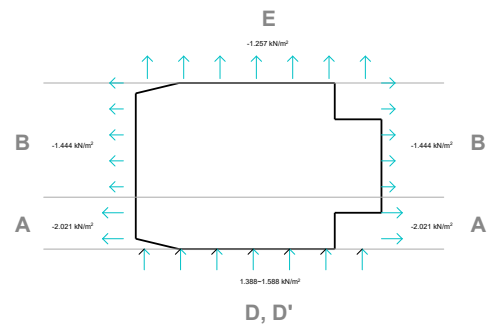
External wind pressure:  $w_e := q_p \cdot c_{pe}$

Internal wind pressure:  $w_i := q_p \cdot c_{pi}$

Net wind pressure (EN1991-1-1-4 §7.2.10)  $w_{net} := w_e - w_i$

Pressure zones determined as EN1991-1-1-4 Fig 7.4 and 7.5:  $e := \min(b, 2 \cdot h) = 25m$

Net wind pressure: Zone A: -2.021 kN/m<sup>2</sup>  
Zone B: -1.444 kN/m<sup>2</sup>  
Zone D: 1.588 kN/m<sup>2</sup>  
Zone D': 1.338 kN/m<sup>2</sup>  
Zone E: -1.257 kN/m<sup>2</sup>



### 3. General considerations on the structural scheme

The scheme proposed consist of a braced frame structure to a central core. A smaller core runs from foundation to rooftop (shaded in blue in Figure 3.1 and 3.2) and a larger core running from basement to level 18 ( shaded in yellow in Fig. 3.2).

#### Level 18-22

Considering that the upper levels will be used as a penthouse the structural scheme tried to optimize flexibility of use by creating two uninterrupted spaces (bay 1 and 3). Columns are placed at the edges and braced to the central core via flat slabs (Figure 3.1). Flat slabs seemed the better option in terms of floor to ceiling clearance, construction and integration with MEP systems.

Columns E5 and E6 were moved internally to avoid a transfer beam on level 17. This produces a simpler and stronger structure without too much interference in Bay 2 that is assumed to be used as a transition space.

#### Level 3-18

Below the upper penthouse the central core expands and incorporates both vertical and horizontal circulation. Slabs and outer columns are braced to it.

On level 17, at the connection of the penthouse levels and the medium part of the building (Fig 3.3), a transfer beam is proposed for:

- solve the connection between slanted columns and vertical structural elements coming from upper floors.
- avoid punching shear reinforcement in the slab
- transfer the axial load of column E4 and C4

Flat slabs are proposed with the exception of lower levels (3-6) between grid 2 and 4 where a two way slab supported by beam is proposed. This is due to the span reaching values above 9m up to 12m. This was considered uneconomical and creating unnecessary complications in comparison to the benefits of a slimmer slab (15-20cm).

#### Level -1 to 3

The structural layout for the lowest level is driven by the request of obtaining spans of minimum 8m. Due to spans above 11m between grid 2 and 4, a system of slab supported by beams was preferred to flat slabs that would generate excessive moments on the columns.

An additional note on columns B7 and F7. The current position was preferred to B8 F8 for structural reasons: the current position is aligned with upper floors while locating them on grid 8 would require a transfer beam. Ultimately the space created at B7 and F7 would not be so of much value considering the location relative to the building.

Due to determined report length, in the following sections only calculation of key structural elements are shown. These were considered the elements that are under the highest structural stress. After this preliminary design a more detailed and optimized design should be carries.

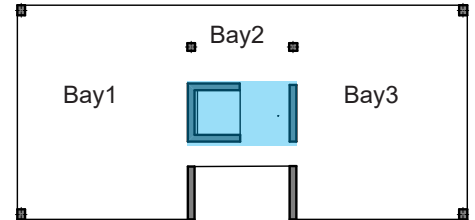


Figure 3.1: diagram of structural scheme for levels 18-22. Shaded area in blue shows the central core

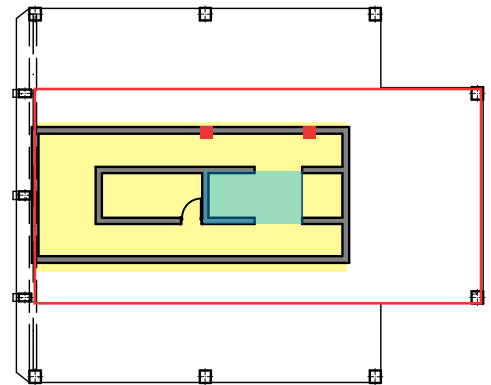


Figure 3.2: diagram of structural scheme for level 17. The red outline represent the layout of the upper floors. Blue shaded area shows the core reaching the roof while yellow shade indicated the core f up to level 18.

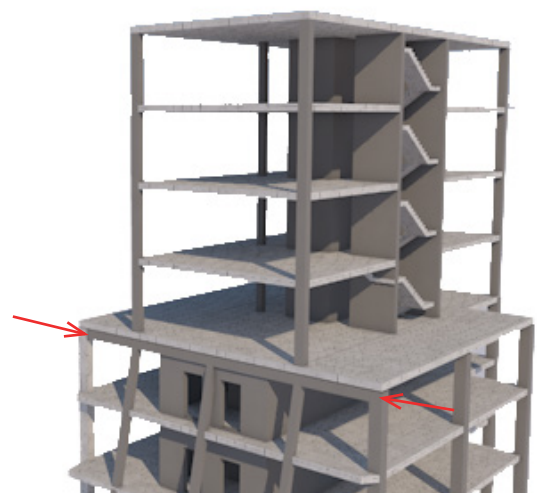


Figure 3.3: position of the transfer beam on level 17

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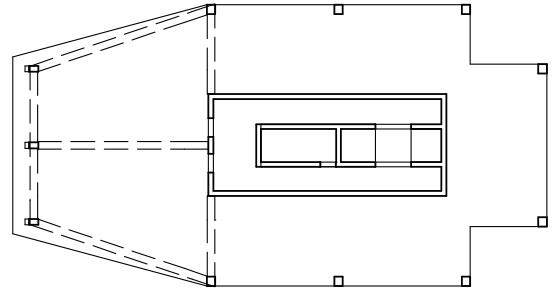


Figure 3.4: diagram of structural scheme for level 3. The structure in front part of the building is made by beam and columns supporting a two way slab. The back of the building hosts flat slabs directly connected to columns.

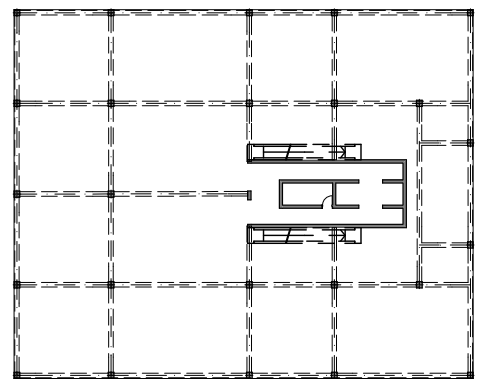


Figure 3.5: diagram of structural scheme for ground and basement levels. One way and two way slabs supported by beams was the chosen structural scheme for this levels due to the longer span in one section

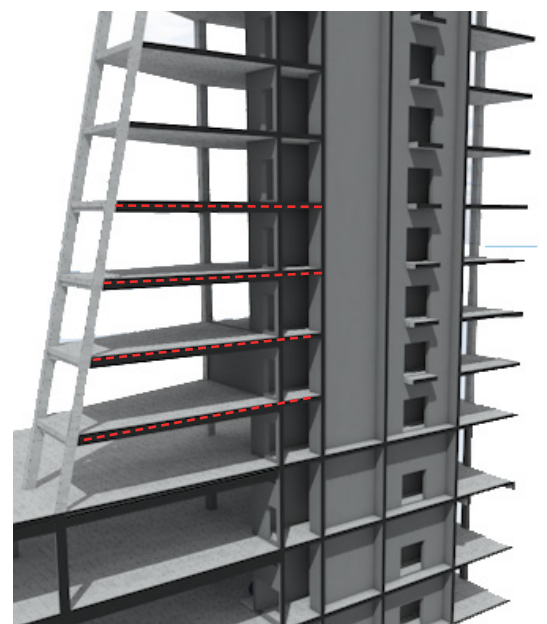


Figure 3.6: the front part of level 3-6 have spans that reach 12m. A flat slab would not be a convenient solution. Two way slabs supported by beams was chosen instead (red dashed lines).

## 4.1 Slab analysis / levels 19-22

The proposed design divides each level into 3 bays: the central one including the core and circulation and two side ones (7.5m x 9m) without any column interruption to allow for maximum flexibility of use. A flat slab of 300mm is proposed to maximize floor height. For construction simplicity the thickness of the slab is constant across the whole floor.

**ELEMENT** Level 22, Slab, Bay 1 long span

**INITIAL PARAMETERS** (EC2 Table 3.1)

$$h_{slab} := 300mm \quad b_{slab} := 7500mm \quad span_{slab} := 9m$$

$$f_{yd} := \frac{500}{1.5} MPa \quad f_{ck} := 30 Mpa \quad f_{cd} := 20$$

$$f_{yk} := 500 \cdot 0.9 \text{ MPa} \quad f_{ctm} := 0.3 \cdot f_{ck}^{.66} = 2.832$$

$$dia_{rebar} := 12mm \quad w_{column} := 400mm$$

**CONCRETE COVER**

Fire protection (EN1992-1-2 Table 5.8, REI 120)  
45mm

Bond (assuming 20 mm bars)

20mm

Durability for XS1 (BS 8500-1:Table A4, IIB-V, IIIA)

35+10=45mm

Cover required for slab is 45mm  $cover := 45mm$

**EFFECTIVE DIMENSIONS**

Effective depth:

$$d := h_{slab} - cover - dia_{rebar} \cdot 0.5 = 249 \cdot mm$$

Effective spans:

$$L_x := 9000mm \quad L_y := 7500mm$$

**LOADINGS**

$$\text{Permanent load: } g_k := h_{slab} \cdot 25 \frac{kN}{m^3} \cdot L_x \cdot L_y = 506.25 \cdot kN$$

$$\text{Variable load } q_k := 2.5 \frac{kN}{m^2} \cdot L_x \cdot L_y = 168.75 \cdot kN$$

$$\text{Cladding load } clad := 2 \frac{kN}{m^2} \quad g_{clad} := clad \cdot 0.25m \cdot L_x$$

Ultimate load according to EN 1990:2002

$$n := 1.35(g_k + g_{clad}) + 1.5 \cdot q_k = 942.638 \cdot kN$$

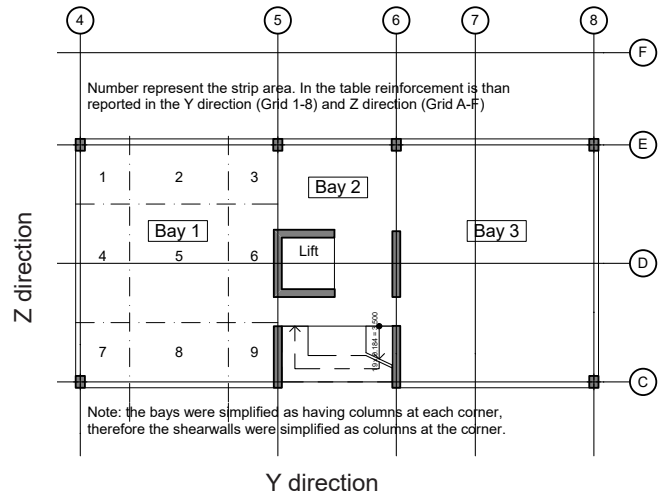


Fig: 2.1 Typical plan for levels 19-22

**MOMENT MID SPAN MIDDLE**

Bending moment at the middle strip end span:  
(Ref: "How to..." Table 3)

$$M_{m\_span} := 0.075 \cdot n \cdot L_x = 636.28 \cdot m \cdot kN$$

$$M_{m\_span} := 516 \cdot kN \cdot m \quad \text{from moment distribution}$$

Middle strip take 0.4 of the load

$$M_{mid} := 0.4 \cdot M_{m\_span} = 206.4 \cdot kN \cdot m$$

$$K := \frac{M_{mid}}{(b \cdot d^2 \cdot f_{ck})} = 0.025$$

$$Z := d \cdot \left[ 0.5 + \left( 0.25 - \frac{K}{1.133} \right)^{0.5} \right] = 243.457 \cdot mm$$

$$\frac{Z}{d} = 0.978 \quad \text{use } Z := 0.95 \cdot d = 236.55 \cdot mm$$

$$A_s := \frac{M_{mid}}{0.87 \cdot f_{yk} \cdot Z} = 2.111 \times 10^3 \quad mm^2$$

$$A_{s\_mm} := \frac{A_s \cdot mm^2}{L_x \cdot 0.5} = 469.204 \cdot \frac{mm^2}{m}$$

$$A_{s\_eff} := 770 \frac{mm^2}{m} \quad \text{H14 at 200 c/c (770 mm}^2\text{)}$$

$$\rho := \frac{A_{s\_eff}}{h_{slab} \cdot 1} = 0.257 \cdot \%$$

## MOMENT MID SPAN COLUMN

Column strip takes 0.6

$$M_{col} := 0.6 \cdot M_{m\_span} = 309.6 \cdot \text{kN} \cdot \text{m}$$

$$K := \frac{M_{col}}{b \cdot d^2 \cdot f_{ck}} = 0.037$$

$$Z := d \cdot \left[ 0.5 + \left( 0.25 - \frac{K}{1.133} \right)^{0.5} \right] = 240.587$$

$$\frac{Z}{d} = 0.966 \quad \text{use} \quad Z := 0.95 \cdot d = 236.55$$

$$A_{s\_tot} := \frac{M_{col}}{0.87 \cdot f_{yk} \cdot Z} = 3.167 \times 10^3 \text{ mm}^2$$

$$A_{s\_mc} := \frac{A_{s\_tot} \cdot \text{mm}^2}{L_x \cdot 0.5} = 703.805 \cdot \frac{\text{mm}^2}{\text{m}}$$

H14 at 175c/c (880 mm2)

## MOMENT SUPPORT SPAN MIDDLE

$$M_{m\_support} := 536 \text{ kN} \cdot \text{m} \quad \text{from moment distribution}$$

Middle strip take 0.4 of the load

$$M_{mid} := 0.4 \cdot M_{m\_support} = 214.4 \cdot \text{kN} \cdot \text{m}$$

$$K := \frac{M_{mid}}{(b \cdot d^2 \cdot f_{ck})} = 0.026$$

$$Z := d \cdot \left[ 0.5 + \left( 0.25 - \frac{K}{1.133} \right)^{0.5} \right] = 243.237 \cdot \text{mm}$$

$$\frac{Z}{d} = 0.977 \quad \text{use} \quad Z := 0.95 \cdot d = 236.55 \cdot \text{mm}$$

$$A_s := \frac{M_{mid}}{0.87 \cdot f_{yk} \cdot Z} = 2.084 \times 10^3 \text{ mm}^2$$

$$A_{s\_mm} := \frac{A_s \cdot \text{mm}^2}{L_x \cdot 0.5} = 463.02 \cdot \frac{\text{mm}^2}{\text{m}}$$

H12 at 200 c/c (565 mm2)

$$A_{s\_eff} := 616 \frac{\text{mm}^2}{\text{m}} \quad \rho := \frac{A_{s\_eff}}{h_{slab} \cdot 1} = 0.205 \cdot \%$$

Note that H14@250 was not chosen to control cracking above 0.3mm as shown below:

## BAR SPACING

$$f_{yk} := 500 \text{ MPa} \quad \gamma_{ms} := 1.14 \quad \psi_2 := 0.3 \quad \delta := 1$$

$$A_s := A_{s\_mm} \quad A_{s\_eff} := 616 \frac{\text{mm}^2}{\text{m}}$$

$$\sigma_z := \frac{f_{yk}}{\gamma_{ms}} \left( \frac{\psi_2 \cdot q_k + g_k}{1.5q_k + 1.35g_k} \right) \cdot \left( \frac{A_s}{A_{s\_eff}} \right) \cdot \frac{1}{\delta} = 196.022 \cdot \text{MPa}$$

From Table 5.6 from BCA2006, maximum distance between bars to avoid crack > 0.3mm:

$$\text{MAX} := 250 \text{ mm}$$

## MOMENT SUPPORT, COLUMN

$$M_{m\_support} := 536 \text{ kN} \cdot \text{m} \quad \text{from moment distribution}$$

Middle strip take 0.6 of the load

$$M_{col} := 0.6 \cdot M_{m\_support} = 321.6 \cdot \text{kN} \cdot \text{m}$$

$$K := \frac{M_{col}}{(b \cdot d^2 \cdot f_{ck})} = 0.038$$

$$Z := d \cdot \left[ 0.5 + \left( 0.25 - \frac{K}{1.133} \right)^{0.5} \right] = 240.248$$

$$\frac{Z}{d} = 0.965 \quad \text{use} \quad Z := 0.95 \cdot d = 236.55$$

$$A_s := \frac{M_{col}}{0.87 \cdot f_{yk} \cdot Z} = 3.125 \times 10^3 \text{ mm}^2$$

$$A_{s\_mm} := \frac{A_s \cdot \text{mm}^2}{L_x \cdot 0.5} = 694.53 \cdot \frac{\text{mm}^2}{\text{m}}$$

H14 at 175 c/c (880 mm2)

$$A_{s\_eff} := 880 \frac{\text{mm}^2}{\text{m}} \quad \rho := \frac{A_{s\_eff}}{h_{slab} \cdot 1} = 0.293 \cdot \%$$

## DEFLECTION

Span to effective ratio,  $\rho=0.3\%$ ,  $f_{ck}=30$   $N := 39.2$   
 "How to..." Table C10

Flat slab, EN1992-1-1 Table 7.4N  $K := 1.2$

Gk/Qk=2.5,  $\psi=0.3$ ,  $\gamma=1.25$   $\sigma_{su} := 255 \text{ MPa}$   
 "How to..." Fig.C3

Redistribution ratio  $\delta := 1.08$

$$A_{s\_mm}$$

$$\sigma_s := \sigma_{su} \cdot \frac{A_{s\_mm}}{A_{s\_eff} \cdot \delta} = 212.969 \frac{1}{\text{m}} \cdot \text{MPa}$$

$b_{eff}/b_w=1$  "How to..." Table C12

No brittle partition "How to..." Table C13

$$F1 := 1 \quad F2 := 1 \quad F3 := \frac{310 \text{ MPa}}{\sigma_s} = 1.456 \text{ m}$$

Allowable deflection  $N \cdot K \cdot F1 \cdot F2 \cdot F3 = 68.472 \text{ m}$

$$\text{Actual} \quad \frac{\text{span}_{slab}}{d \cdot \text{mm}} = 36.145 \quad \text{OK}$$

## Crack control

Steel stress under quasi permanent loading:

$$\sigma_z := \frac{f_{yk}}{\gamma_{ms}} \left( \frac{\psi_2 \cdot q_k + g_k}{1.5q_k + 1.35g_k} \right) \cdot \left( \frac{A_{s\_mm}}{A_{s\_eff}} \right) \cdot \frac{1}{\delta} = 217.803 \text{ MPa}$$

Maximum diameter 20mm or distance 225mm.

H28@122 acceptable.

### PUNCHING SHEAR

$$w_{col} := 350\text{mm} \quad b_{col} := 450\text{mm}$$

$$u_0 := (w_{col} + b_{col}) \cdot 2 \quad \beta := 1.5$$

As per Figure 6.21N in EN 1992-1-1-2004

$$n_{m2} := \frac{n}{L_x \cdot L_y} = 13.965 \cdot \frac{\text{kN}}{\text{m}^2}$$

$$V_{Ed} := \left( \frac{L_x \cdot L_y}{2} \cdot \frac{L_y}{2} - w_{col} \cdot b_{col} \right) \cdot n_{m2} \cdot \beta = 350.19 \cdot \text{kN}$$

$$\frac{V_{Ed}}{u_0 \cdot d} = 0.879 \cdot \text{MPa}$$

$$v := 0.6 \cdot \left( 1 - \frac{f_{ck}}{250} \right) = 0.528 \quad f_{cd} := 1.1 \cdot \frac{f_{ck}}{1.5} = 20$$

$$V_{Rd} := 0.5 \cdot v \cdot f_{cd} = 5.28$$

No additional reinforcement needed

### PUNCHING SHEAR AT 2d

$$u_1 := 2 \cdot (b_{col} + w_{col}) + 2 \cdot \pi \cdot 2 \cdot d = 4.729\text{m} \quad \gamma_c := 1.5$$

$$v_{USF} := n_{m2} \cdot \frac{L_x \cdot L_y}{2} \cdot \frac{L_y}{2} \dots = 252.104 \cdot \text{kN}$$

$$+ n_{m2} \cdot \left[ w_{col} \cdot 2 \cdot d \dots + b_{col} \cdot d \cdot 2 + \pi \cdot (2 \cdot d)^2 \right]$$

$$v_{u1} := \frac{1.15 \cdot v_{USF}}{u_1 \cdot d} = 0.246 \cdot \text{MPa} \quad \text{Stress at } u_1$$

$$\rho_{lx} := \frac{1130}{d \cdot 1000} = 4.538 \times 10^{-3}$$

$$\rho_{ly} := \frac{1130}{d \cdot 1000} = 4.538 \times 10^{-3}$$

$$C_{Rd_c} := \frac{0.18}{\gamma_c} = 0.12$$

$$k := \left( 1 + \frac{200}{d} \right)^{0.5} = 1.343 \quad \rho_1 := (\rho_{lx} \cdot \rho_{ly})^{0.5}$$

$$v_{Rd_c} := C_{Rd_c} \cdot k \cdot (100 \cdot \rho_1 \cdot f_{ck})^{0.33} \cdot \text{MPa} = 0.381 \cdot \text{MPa}$$

$$V_{Rd_c} := v_{Rd_c} \cdot u_1 \cdot d = 449.155 \cdot \text{kN}$$

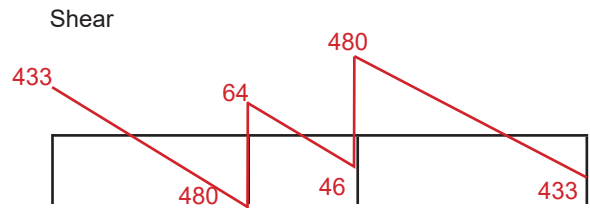
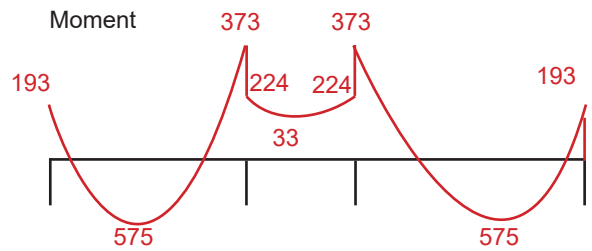
$$v_{USF} = 252.104 \cdot \text{kN}$$

Punching shear reinforcement not needed

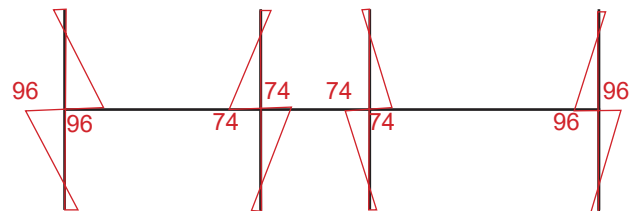
### Grid E / Level 19-22

Loading

Q <sub>k</sub> 22.5 kN/m	Q <sub>k</sub> 8.2	Q <sub>k</sub> 22.5 kN/m
G <sub>k</sub> 56.2 kN/m	G <sub>k</sub> 20	G <sub>k</sub> 56.2 kN/m
7.5m	4m	7.5m



Column moment

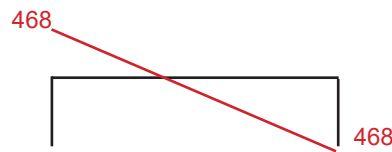


### Grid 4 / Level 19

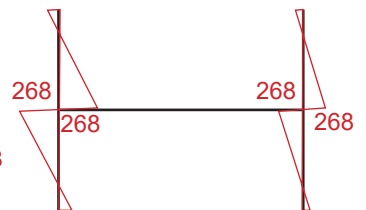
Q <sub>k</sub> 18 kN/m
G <sub>k</sub> 56 kN/m
9m



Shear



Column moment



### Summary for slab analysis levels 19-22

Slab type: flat slab across the whole level  
Thickness: 300mm across the whole level for ease of construction

Punching shear reinforcement is not needed near the supports. Reinforcement is estimated as follows. Refer to Figure 2.1 for strip numbering. Note: redistributing reinforcement within the strips and according to code would be needed.

Bay	Direction	Strip			
		1,3,7,9	2,8	4,6	5
1,3	Y	H10@200	H18@150	H8@200	H14@125
	Z	H16@150	H10@150	H10@125	H10@150
2	Y	H8@125	H8@150	H8@150	H8@150
	Z	H8@150	H8@150	H8@150	H8@150



## 4.2 Column design levels 19-22

### Column E5 and E6

Analysis for internal column E5 and E6. The structural layout (Fig. 4.2.1) was simplified. The single bays (indicated as 45 and 56 in the calculation) are simplified as shown in Fig 4.2.2. This simplification was only used for the moment calculation. The structure is still considered braced to the central core. The size of the column (350mm) is limited by fire regulation.

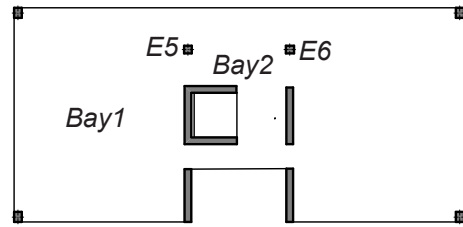


Figure 4.2.1: diagram of structural scheme for levels 18-22

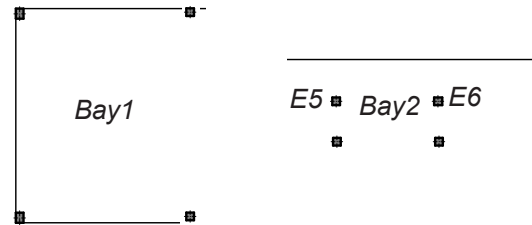


Figure 4.2.2: simplified scheme for bay 4-5 (left) and bay 5-6 and column analysis. Note the frame is still considered braced.

**COLUMN** Level 18 Column E6

#### DIMENSIONS AND MATERIAL CHARACTERISTICS

Column

$$y := 350\text{mm} \quad z := 400\text{mm} \quad h_{col} := 3.5\text{m}$$

Slab Grid 4-5

$$y_{45} := 7.5\text{m} \quad z_{45} := 9\text{m} \quad h_{slab} := .30\text{m}$$

Slab Grid 5-6

$$y_{56} := 4\text{m} \quad z_{56} := 3.3\text{m}$$

$$dia_{bar} := 12\text{mm} \quad dia_{link} := 8\text{mm}$$

$$f_{cd} := \frac{30}{1.5}\text{MPa} \quad f_{yd} := \frac{500}{1.5}\text{MPa}$$

#### COVER

As per EN1992-1-2 Table 5.2a and REI120 45mm  
cover := 45mm

#### ACTIONS

Load from slab weight, variable load and cladding.  
Y direction grid 4-6, Z direction grid E to F

$$g_k := 25 \frac{\text{kN}}{\text{m}^3} \cdot h_{slab} = 7.5 \cdot \frac{\text{kN}}{\text{m}^2}$$

$$q_k := 2.5 \frac{\text{kN}}{\text{m}^2} = 2.5 \cdot \frac{\text{kN}}{\text{m}^2} \quad q_{k2} := 5 \frac{\text{kN}}{\text{m}^2}$$

$$g_{k45} := z_{45} \cdot 1.35 \cdot g_k = 91.125 \cdot \frac{\text{kN}}{\text{m}}$$

$$q_{k45} := z_{45} \cdot 1.5 \cdot q_k = 33.75 \cdot \frac{\text{kN}}{\text{m}}$$

$$g_{k56} := z_{56} \cdot 1.35 \cdot g_k = 33.413 \cdot \frac{\text{kN}}{\text{m}}$$

$$q_{k56} := z_{56} \cdot 1.5 \cdot q_{k2} = 24.75 \cdot \frac{\text{kN}}{\text{m}}$$

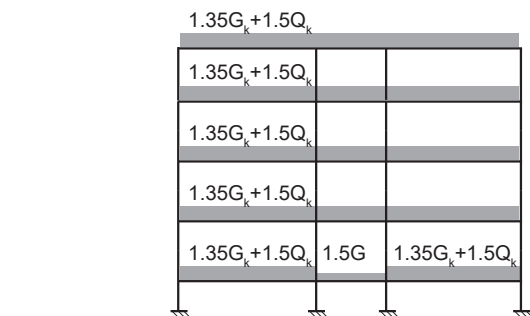
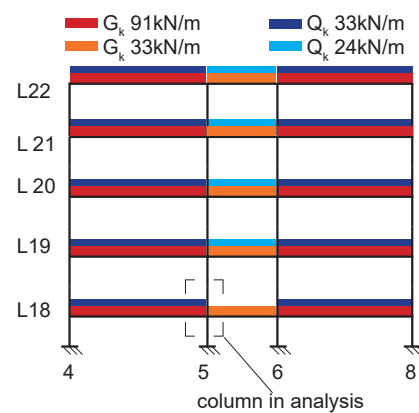


Figure 4.2.3 combination of actions



Figure 4.2.4 distribution factors along Y (Grid 5) and Z (Grid E)

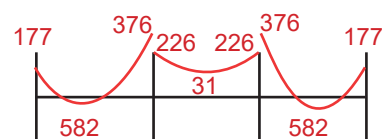


Figure 4.2.5: moment distribution along Y (Grid 5)

## Axial Load

Area supported by the column on bay1 (grid 4-5):

$$A_{45} := z_{45} \cdot y_{45} \cdot 0.25 = 16.875 \text{ m}^2$$

$$A_{56} := z_{56} \cdot y_{56} \cdot 0.25 = 3.3 \text{ m}^2$$

Load per floor:

$$UDL_{56} := A_{56} \cdot (1.5g_k + 1.5q_{k2}) = 61.875 \cdot \text{kN}$$

$$UDL_{45} := A_{45} \cdot (1.35g_k + 1.5q_k) = 234.141 \cdot \text{kN}$$

Load from column

$$g_{col} := y \cdot z \cdot 4 \cdot 3.5 \text{ m} \cdot 25 \frac{\text{kN}}{\text{m}^3} = 49 \cdot \text{kN}$$

Load from cladding:

$$g_{clad} := 2.5 \frac{\text{kN}}{\text{m}^2} \cdot \left( \frac{y_{45} + y_{56}}{2} \right) \cdot 3.5 \cdot 4 \text{ m} = 201.25 \cdot \text{kN}$$

$$N_{Ed} := 5 \cdot (UDL_{56} + UDL_{45}) \dots = 1.706 \times 10^3 \cdot \text{kN} \\ + -(A_{56} \cdot 1.5q_{k2}) + g_{col} \dots \\ + g_{clad}$$

## **DISTRIBUTION FACTORS**

Stiffness, upper column  $E_{uc} := \frac{y^3 \cdot z}{h_{col}} = 4.9 L$

Stiffness, lower column  $E_{lc} := E_{uc}$

Stiffness, slab grid 45:

$$E_{sl45} := z_{45} \cdot \frac{h_{slab}^3}{y_{45}} = 32.4 L$$

Stiffness, slab grid 56:

$$E_{sl56} := z_{56} \cdot \frac{h_{slab}^3}{y_{56}} = 22.275 L$$

Distribution factor upper and lower column

$$DF_{uc} := \frac{E_{uc}}{E_{lc} + E_{uc} + E_{sl45} + E_{sl56}} = 0.076$$

Distribution factor Ydirection slab 45

$$DF_{sl45} := \frac{E_{sl45}}{E_{lc} + E_{uc} + E_{sl45} + E_{sl56}} = 0.503$$

Distribution factor Y direction slab 56

$$DF_{sl56} := \frac{E_{sl56}}{E_{lc} + E_{uc} + E_{sl45} + E_{sl56}} = 0.345$$

Distribution factor Z direction column

$$DF_{uc\_z} := \frac{E_{uc}}{E_{lc} + E_{uc} + E_{sl45}} = 0.116$$

## **SLENDERNESS CHECK**

$$\text{factor} := 0.85$$

From BS8110:Part 1:1997

$$l_0 := (3500 \text{ mm} - 300 \text{ mm}) \cdot \text{factor} = 2.72 \text{ m}$$

$$\lambda_z := 3.46 \cdot \frac{l_0}{z} = 23.528 \quad \lambda_y := 3.46 \cdot \frac{l_0}{y} = 26.889$$

$$A := 0.7$$

A.s taken from end of calculation:

$$\omega := \frac{A_s \cdot f_{yd}}{y \cdot z \cdot f_{cd}} = 0.292 \quad B := (1 + 2 \cdot \omega)^{0.5} = 1.259$$

Worst case for braced structures

$$C := 1.7$$

$$n := \frac{N_{Ed}}{y \cdot z \cdot \text{factor} \cdot f_{cd}} = 0.717$$

$$\lambda_{lim} := 20 \cdot \frac{A \cdot B \cdot C}{n^{0.5}} = 35.395$$

Column not slender since  $\lambda_{lim} > \lambda_y$  and  $\lambda_z$

## **MOMENTS IN Y DIRECTION**

From moment distribution (see Table 4.2.1):

$$M_{Edyy} := 74 \text{ kN} \cdot \text{m}$$

On the z direction

$$UDL_{z56} := y_{56} \cdot (1.35 \cdot g_k + 1.5 \cdot q_{k2}) = 70.5 \cdot \frac{\text{kN}}{\text{m}}$$

On the Z direction the cantilever produces a moment opposite and greater than the internal part of the slab

$$M_{Edzz} := \frac{\left( \frac{z_{56}}{2} \cdot UDL_{56} \right)}{12} \dots = -93.586 \cdot \text{kN} \cdot \text{m} \\ + \frac{-z_{56}}{2} \cdot UDL_{56}$$

$$M_{Edzz} := -M_{Edzz}$$

## DESIGN REINFORCEMENT

$$f_{ck} := 30 \text{ MPa}$$

$$f_{yk} := 500 \frac{\text{N}}{\text{mm}^2}$$

$$\frac{M_{Edzz}}{y \cdot z^2 \cdot f_{ck}} = 0.056$$

$$\frac{N_{Ed}}{y \cdot z \cdot f_{ck}} = 0.406$$

$$z = 0.4 \text{ m}$$

$$d_2 := \text{cover} + dia_{link} + dia_{bar} \cdot 0.5 = 0.059 \text{ m}$$

$$\frac{d_2}{z} = 0.147$$

From chart with  $d/z$  of 0.15  $A_s$   $F_{yk}$  /  $b h f_{ck}$   
(Harrison2007a, p39)

$$\text{ratio} := 0.05$$

$$A_s := \frac{\text{ratio} \cdot y \cdot z \cdot f_{ck}}{f_{yk}} = 420 \cdot \text{mm}^2$$

8 bars H12 (905  $\text{mm}^2$ )

Crushing load of a truly loaded column  
may be taken as: (Mosley, p.267)

$$N_{ud} := 0.567 \cdot f_{ck} \cdot y \cdot z + 0.87 \cdot A_s \cdot f_{yk} = 2.564 \times 10^3 \cdot \text{kN}$$

$$N_{Ed} = 1.706 \times 10^3 \cdot \text{kN}$$

Minimum area of steel needs to be above 0.002  $A_c$

$$A_{s_{min}} := 0.002 \cdot y \cdot z = 280 \cdot \text{mm}^2 \quad \frac{A_s}{z \cdot y} = 0.3 \cdot \%$$

## DESIGN FIRE RESISTANCE

check that effective length < 3m

$$l_0 := (3.1 \text{ m} - 0.3 \text{ m}) \cdot 0.85 = 2.38 \text{ m} \quad \text{OK}$$

$$\text{check } e < e_{\max} \quad e := \frac{M_{Edyy}}{N_{Ed}} = 0.043 \text{ m}$$

$$e_{\max} := 0.15 \cdot z = 0.06 \text{ m} \quad \text{OK}$$

$$\text{Check reinforcement } < 4\% \quad \frac{A_s}{z \cdot y} = 0.3 \cdot \% \quad \text{OK}$$

## CHECK BIAXIAL BENDING

$$N_{Ed} = 1.706 \times 10^6 \text{ N}$$

$$e_z := \frac{M_{Edzz}}{N_{Ed}} = 54.871 \cdot \text{mm} \quad e_y := \frac{M_{Edyy}}{N_{Ed}} = 43.387 \cdot \text{mm}$$

$$\frac{e_y}{e_z} = 0.791 \quad \text{between 0.2 and 5, design for biaxial bending needs to be checked}$$

From chart obtain ratio of  $A_s$   $f_{yk}$  /  $b h f_{ck}$

Previously calculated reinforcement not enough,  
8 H12 (905  $\text{mm}^2$ ) used instead

$$A_{s_{eff}} := 905 \text{ mm}^2 \quad A_{s_{eff}} \cdot \frac{f_{yk}}{y \cdot z \cdot f_{ck}} = 0.108$$

$$\frac{N_{Ed}}{z \cdot y \cdot f_{ck}} = 0.406 \quad \frac{d_2}{y} = 0.169$$

$$f_{chart} := 0.088$$

$$M_{Rd} := f_{chart} \cdot y \cdot z^2 \cdot f_{ck} = 147.84 \cdot \text{kN} \cdot \text{m}$$

$$N_{Rd} := z \cdot y \cdot f_{cd} \cdot 0.85 + A_{s_{eff}} \cdot f_{yd} = 2.682 \times 10^3 \cdot \text{kN}$$

Value for  $a$  obtained from chart (Harrison2007a, Table 5):

$$\frac{N_{Ed}}{N_{Rd}} = 0.636 \quad a := 1 + \left( \frac{N_{Ed}}{N_{Rd}} - 0.1 \right) \cdot \frac{0.5}{0.6} = 1.447$$

$$\left( \frac{M_{Edzz}}{M_{Rd}} \right)^a + \left( \frac{M_{Edyy}}{M_{Rd}} \right)^a = 0.884 \quad \text{Acceptable}$$

## CHECK REINFORCEMENT

$$\text{As minimum} \quad \frac{0.10 N_{Ed}}{f_{yd}} = 511.673 \cdot \text{mm}^2$$

$$\text{Reinforcement to area ratio} \quad \frac{A_{s_{eff}}}{y \cdot z} = 0.646 \cdot \%$$

Reinforcement is above 0.2% and below 4% and above  $A_s$  minimum.

## TRANSVERSE REINFORCEMENT

Ref. EC2 9.5.3&NA

Diameter of bar should exceed 6m of 1/4 of reinforcement bars

$$dia_{min} := dia_{bar} \cdot 0.25 = 3 \cdot \text{mm}$$

**Diameter 6mm**

Spacing given by the minimum

$$20 \cdot dia_{bar} = 240 \cdot \text{mm}$$

$$y = 350 \cdot \text{mm}$$

**H6 @ 240 mm**

$$400 \text{ mm} = 400 \cdot \text{mm}$$

## Column E4, C4, E8, C8

Analysis for corner columns. The structural layout (Fig. 4.2.1) was simplified. Unlike for the internal columns, no simplification was done. Moments were analysed using equivalent frame method.

**COLUMN** Level 18 Column E4

### DIMENSIONS AND MATERIAL CHARACTERISTICS

Column

$$y := 350\text{mm} \quad z := 400\text{mm} \quad h_{col} := 3.5\text{m}$$

Slab Grid 4-5

$$y_{45} := 7.5\text{m} \quad z_{45} := 9\text{m} \quad h_{slab} := .30\text{m}$$

$$dia_{bar} := 14\text{mm} \quad dia_{link} := 6\text{mm}$$

$$f_{cd} := \frac{30}{1.5}\text{MPa} \quad f_{yd} := \frac{500}{1.5}\text{MPa}$$

### COVER

As per EN1992-1-2 Table 5.2a and REI120 45mm  
cover := 45mm

### ACTIONS

Load from slab weight, variable load and cladding.  
Y direction grid 4-6, Z direction grid E to F

$$g_k := 25 \frac{\text{kN}}{\text{m}^3} \cdot h_{slab} = 7.5 \cdot \frac{\text{kN}}{\text{m}^2}$$

$$q_k := 2.5 \frac{\text{kN}}{\text{m}^2} = 2.5 \cdot \frac{\text{kN}}{\text{m}^2} \quad q_{k2} := 5 \frac{\text{kN}}{\text{m}^2}$$

$$g_{k45} := z_{45} \cdot 1.35 \cdot g_k = 91.125 \cdot \frac{\text{kN}}{\text{m}}$$

$$q_{k45} := z_{45} \cdot 1.5 \cdot q_k = 33.75 \cdot \frac{\text{kN}}{\text{m}}$$

### Axial Load

Area supported by the column on bay1 (grid 4-5):

$$A_{45} := z_{45} \cdot y_{45} \cdot 0.25 = 16.875\text{m}^2$$

Load per floor:

$$UDL_{45} := A_{45} \cdot (1.35g_k + 1.5q_k) = 234.141 \cdot \text{kN}$$

Load from column

$$g_{col} := y \cdot z \cdot 4 \cdot 3.5\text{m} \cdot 25 \frac{\text{kN}}{\text{m}^3} = 49 \cdot \text{kN}$$

Load from cladding:

$$g_{clad} := 2.5 \frac{\text{kN}}{\text{m}^2} \cdot \left( \frac{y_{45} + z_{45}}{2} \right) \cdot 3.5 \cdot 4\text{m} = 288.75 \cdot \text{kN}$$

$$N_{Ed} := 5 \cdot (UDL_{45}) + g_{col} + g_{clad} = 1.508 \times 10^3 \cdot \text{kN}$$

### SLENDERNESS CHECK

factor := 0.85 From BS8110:Part 1:1997

$$l_0 := (3500\text{mm} - 300\text{mm}) \cdot \text{factor} = 2.72\text{m}$$

$$\lambda_z := 3.46 \cdot \frac{l_0}{z} = 23.528 \quad \lambda_y := 3.46 \cdot \frac{l_0}{y} = 26.889$$

$$A := 0.7$$

As taken from end of calculation:

$$A_s := 1.23 \cdot 10^3 \text{mm}^2$$

$$\omega := \frac{A_s \cdot f_{yd}}{y \cdot z \cdot f_{cd}} = 0.146 \quad B := (1 + 2 \cdot \omega)^{0.5} = 1.137$$

Worst case for braced structures

$$C := 1.7$$

$$n := \frac{N_{Ed}}{y \cdot z \cdot \text{factor} \cdot f_{cd}} = 0.634$$

$$\lambda_{lim} := 20 \cdot \frac{A \cdot B \cdot C}{n^{0.5}} = 33.992$$

Column not slender since  $\lambda_{lim} > \lambda_y$  and  $\lambda_z$

### MOMENTS

From moment distribution (see table 4.2.1)  
the column would receive a moment in Y direction of:

$$M_{Edyy} := 96\text{kN} \cdot \text{m}$$

On the Z direction the moment would be:

$$M_{Edzz} := 133\text{kN} \cdot \text{m}$$

Transfer to edge and corner column, both upper and lower, is limited to  $M_{max}$   
(and therefore lower column to  $M_{max}/2$ ):

$$d_{slab} := 245\text{mm}$$

$$M_{max} := 0.17 \cdot (z + y) \cdot d_{slab}^2 \cdot f_{ck} = 229.596 \cdot \text{kN} \cdot \text{m}$$

Therefore none of the moments is greater than maximum value.

## DESIGN REINFORCEMENT

$$f_{ck} := 30 \text{ MPa}$$

$$f_{yk} := 500 \frac{\text{N}}{\text{mm}^2}$$

$$\frac{M_{Edzz}}{y \cdot z^2 \cdot f_{ck}} = 0.079$$

$$\frac{N_{Ed}}{y \cdot z \cdot f_{ck}} = 0.359$$

$$z = 0.4 \text{ m}$$

$$d_2 := \text{cover} + \text{dia}_{link} + \text{dia}_{bar} \cdot 0.5 = 0.058 \text{ m}$$

$$\frac{d_2}{z} = 0.145$$

From chart with  $d/z$  of 0.15  $A_s F_{yk} / b h f_{yk}$   
(Harrison2007a, p39)

$$\text{ratio} := 0.06$$

$$A_s := \frac{\text{ratio} \cdot y \cdot z \cdot f_{ck}}{f_{yk}} = 504 \cdot \text{mm}^2$$

8 bars H14 (905mm<sup>2</sup>)

Crushing load of a truly loaded column  
may be taken as: (Mosley, p.267)

$$N_{ud} := 0.567 \cdot f_{ck} \cdot y \cdot z + 0.87 \cdot A_s \cdot f_{yk} = 2.601 \times 10^3 \cdot \text{kN}$$

$$N_{Ed} = 1.508 \times 10^3 \cdot \text{kN}$$

Minimum area of steel needs to be above 0.002Ac

$$A_{s_{min}} := 0.002 \cdot y \cdot z = 280 \cdot \text{mm}^2 \quad \frac{A_s}{z \cdot y} = 0.36\%$$

## DESIGN FIRE RESISTANCE

check that effective length <3m

$$l_0 := (3.1 \text{ m} - 0.3 \text{ m}) \cdot 0.85 = 2.38 \text{ m} \quad \text{OK}$$

$$\text{check } e < e_{\max} \quad e := \frac{M_{Edyy}}{N_{Ed}} = 0.064 \text{ m}$$

$$e_{\max} := 0.15 \cdot z = 0.06 \text{ m} \quad \text{OK}$$

$$\text{Check reinforcement } < 4\% \text{ and above } 0.2\% \quad \frac{A_s}{z \cdot y} = 0.36\% \quad \text{OK}$$

## CHECK BIAXIAL BENDING

$$N_{Ed} = 1.508 \times 10^3 \cdot \text{kN}$$

$$e_z := \frac{M_{Edzz}}{N_{Ed}} = 88.17 \cdot \text{mm} \quad e_y := \frac{M_{Edyy}}{N_{Ed}} = 63.641 \cdot \text{mm}$$

$$\frac{e_y}{e_z} = 0.722 \quad \text{between } 0.2 \text{ and } 5, \text{ design for biaxial bending needs to be checked}$$

From chart obtain ratio of  $A_s f_{yk} / b h f_{ck}$

Previously calculated reinforcement not enough,  
8 H14 (1230 mm<sup>2</sup>) used instead

$$A_{s_{eff}} := 1230 \text{ mm}^2 \quad A_{s_{eff}} \cdot \frac{f_{yk}}{y \cdot z \cdot f_{ck}} = 0.146$$

$$\frac{N_{Ed}}{z \cdot y \cdot f_{ck}} = 0.359 \quad \frac{d_2}{y} = 0.166$$

$$f_{chart} := 0.11$$

$$M_{Rd} := f_{chart} \cdot y \cdot z^2 \cdot f_{ck} = 184.8 \cdot \text{kN} \cdot \text{m}$$

$$N_{Rd} := z \cdot y \cdot f_{cd} \cdot 0.85 + A_{s_{eff}} \cdot f_{yd} = 2.79 \times 10^3 \cdot \text{kN}$$

Value for  $a$  obtained from chart (Harrison2007a, Table 5):

$$\frac{N_{Ed}}{N_{Rd}} = 0.541 \quad a := 1 + \left( \frac{N_{Ed}}{N_{Rd}} - 0.1 \right) \cdot \frac{0.5}{0.6} = 1.367$$

$$\left( \frac{M_{Edzz}}{M_{Rd}} \right)^a + \left( \frac{M_{Edyy}}{M_{Rd}} \right)^a = 1.046 \quad \text{Acceptable}$$

## CHECK REINFORCEMENT

$$\text{As minimum} \quad \frac{0.10 N_{Ed}}{f_{yd}} = 452.536 \cdot \text{mm}^2$$

$$\text{Reinforcement to area ratio} \quad \frac{A_{s_{eff}}}{y \cdot z} = 0.879\%$$

Reinforcement is above 0.2% and below 4% and above  $A_s$  minimum.

## TRANSVERSE REINFORCEMENT

Ref. EC2 9.5.3&NA

Diameter of bar should exceed 6m of 1/4 of reinforcement bars

$$\text{dia}_{min} := \text{dia}_{bar} \cdot 0.25 = 3.5 \cdot \text{mm}$$

**Diameter 6mm**

Spacing given by the minimum

$$20 \cdot \text{dia}_{bar} = 280 \cdot \text{mm}$$

$$y = 350 \cdot \text{mm}$$

$$400 \text{ mm} = 400 \cdot \text{mm}$$

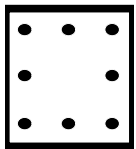
**H6 @ 240 mm**

Table 4.2.1: moment distribution along Y direction (Grid E)

Load G /m2	7.25		7.25		7.25					
Load Q/m2	2.5		5		2.5					
Depth	9		3.3		9					
span	7.5		4		7.5					
Load kN/m	121.8		32.3		121.8					
Load kN	913.8		129.2		913.8					
Shear	913.8		129.2		913.8					
support	E8		E6		E5		E4			
	Column	Slab 86	slab 68	Column	Slab 65	slab 56	Column	Slab 54	slab 45	Column
distribution	24%	76%	50%	15%	35%	35%	15%	50%	76%	24%
FEM	571.1		43.1		571.1					
Moment	571.1	-571.1	43.1	-43.1	571.1	-571.1				
Balance	-137.07	-434.0	264.0	79.2	184.8	-184.8	-79.2	-264.0	434.0	137.1
Distribute										
Carry over		132.0	-217.0		-92.4	92.4		217.0	-132.0	
Balance										
Distribute	-31.68	-100.3	154.7	46.4	108.3	-108.3	-46.4	-154.7	100.3	31.7
Carry over		77.4	-50.2		-54.2	54.2		50.2	-77.4	
Balance										
Distribute	-18.57	-58.8	52.2	15.6	36.5	-36.5	-15.6	-52.2	58.8	18.6
Carry over		26.1	-29.4		-18.3	18.3		29.4	-26.1	
Balance										
Distribute	-6.26	-19.8	23.8	7.1	16.7	-16.7	-7.1	-23.8	19.8	6.3
<b>Total</b>	<b>-193.57</b>	<b>193.6</b>	<b>-373.0</b>	<b>148.4</b>	<b>224.6</b>	<b>-224.6</b>	<b>-148.4</b>	<b>373.0</b>	<b>-193.6</b>	<b>193.6</b>

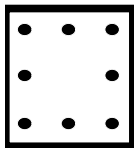
## Column design summary

Column E4,C4, E8,C8



8 H14  
H6 links at 200  
350 x 400mm  
 $f_{ck} = 30\text{MPa}$

Column E5,E6



8 H12  
H6 links at 240  
350 x 350mm  
 $f_{ck} = 30\text{MPa}$

### 4.3 Slab analysis / levels 3-18

Slabs between grid 2 and 4 were initially evaluated as flat slabs. The spans required in lower levels (3 to 6) are in a range (9.5-12m) outside the optimal. The difference in height between a flat slab and slab+beam would not be significant with the disadvantage of having a smaller clearance within the bay.

Bay 1 was then changed to a slab and beam system and analysed as a two way slab. The geometry was simplified into a rectangular shape of 6.5 x 11.5m. It was assumed that the slab has fixity at the corners to prevent torsion and uplifting. Calculation are based on Example 8.5.2 from Mosley (2012). A summary of reinforcement is shown in Table 4.3.

Bays within grid 4 and 8 are proposed as flat slabs considering the reduced spans that allow to take full advantage of the reduced thickness of this type of structure. Reinforcement for Bay 2 is shown in Table 4.3. Calculation follows the same procedure as for upper levels and are not shown in this document. Refer to previous pages.

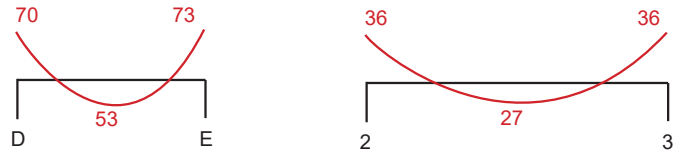


Fig: 4.3.2: diagram of moments for Bay 1 (two way slab)

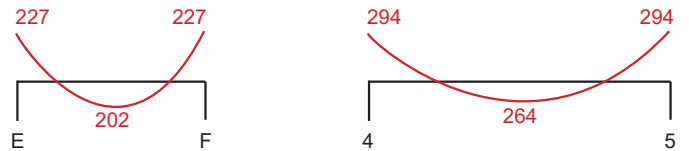


Fig: 4.3.3: diagram of moments for Bay 2 (flat slab)

Table: 4.3: summary of reinforcement for Bay 1 and 2

Bay	Direction	Strip			
		1,3,7,9	2,8	4,6	5
1	Y	H14@200	H10@225	H14@275	H10@225
	Z	H14@200	H14@200	H14@250	H14@250
2	Y	H10@200	H10@150	H10@200	H10@150
	Z	H8@150	H8@150	H8@150	H8@150

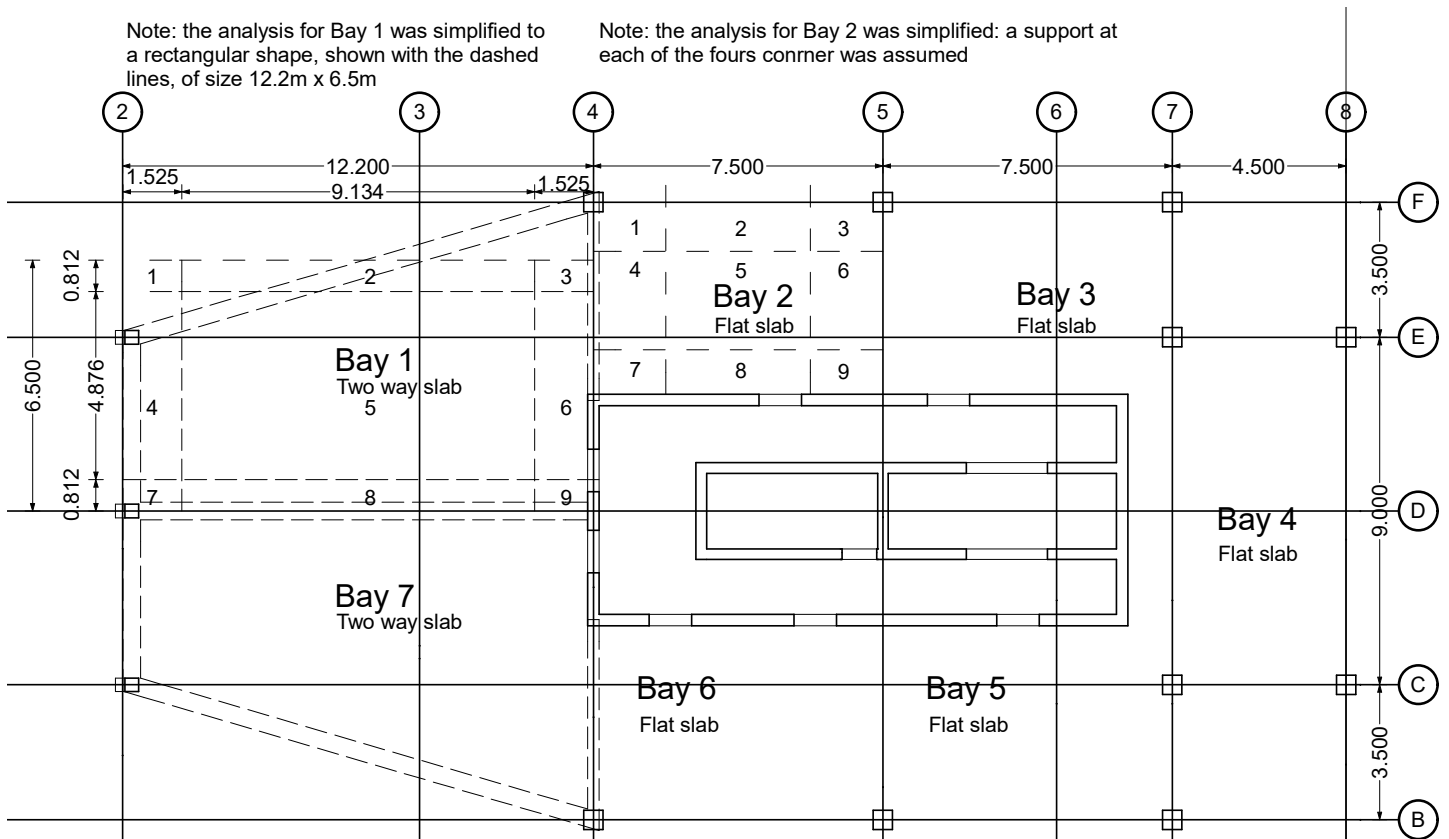


Figure 4.3.1: ceiling plan of level 2

## TWO WAY SLAB LEVEL 3 (as per Brooker2006)

The irregular shape of the slab is approximated to a rectangular one of:

Dimensions:

$$l_x := 6.5m \quad l_y := 12.2m \quad h_{sl} := \frac{l_y}{36} = 0.339m \quad \frac{l_y}{l_x} = 1.877$$

Effective depth:

$$h_{sl} := 350mm \quad d := h_{sl} - 45mm - 8mm = 0.297m$$

### Coefficients for restrained slab (T3.14 BS8110)

Short span, continuous edge:  $\beta_{xe} := 0.087$

Short span, mid-span:  $\beta_{xm} := 0.065$

Long span, continuous edge:  $\beta_{ye} := 0.045$

Long span, mid-span:  $\beta_{ym} := 0.034$

### ULTIMATE LOAD

Imposed load

$$g_k := h_{sl} \cdot 25 \frac{kN}{m^3} = 8.75 \frac{kN}{m^2} \quad q_k := 5 \frac{kN}{m^2}$$

Ultimate load:  $n := 1.35 \cdot g_k + 1.5 \cdot q_k = 19.313 \frac{kN}{m^2}$

### MOMENT AT EDGE, SHORT SPAN

$$M := \beta_{xe} \cdot n \cdot l_x^2 = 70.988 \cdot kN \cdot m \quad b := 1000$$

$$f_{ck} := 30MPa \quad f_{yk} := \frac{500}{1.15} MPa$$

$$K := \frac{M}{(b \cdot d^2 \cdot f_{ck})} = 0.027$$

$$Z := d \cdot \left[ 0.5 + \left( 0.25 - \frac{K}{1.133} \right)^{0.5} \right] = 289.7 mm$$

$$\frac{Z}{d} = 0.976 \quad \text{Design for 0.95} \quad Z := 0.95 \cdot d$$

$$A_s := \frac{M}{0.87 \cdot f_{yk} \cdot Z} = 665.14 \frac{s^2 \cdot mm^2}{kg \cdot m}$$

### H14 @200 (770mm<sup>2</sup>)

### MOMENT AT MIDSPAN SHORT SPAN

$$M := \beta_{xm} \cdot n \cdot l_x^2 = 53.037 \cdot kN \cdot m \quad b := 1000$$

$$f_{ck} := 35MPa \quad f_{yk} := \frac{500}{1.15} MPa$$

$$K := \frac{M}{(b \cdot d^2 \cdot f_{ck})} = 0.017$$

$$Z := d \cdot \left[ 0.5 + \left( 0.25 - \frac{K}{1.133} \right)^{0.5} \right] = 292 mm$$

$$\frac{Z}{d} = 0.985 \quad \text{Design for 0.95} \quad Z := 0.95 \cdot d$$

$$A_s := \frac{M}{0.87 \cdot f_{yk} \cdot Z} = 496.944 \frac{mm^2}{m}$$

### H14 @250 (616mm<sup>2</sup>)

### MOMENT AT EDGE, LONG SPAN

$$M := \beta_{ye} \cdot n \cdot l_x^2 = 36.718 \cdot kN \cdot m \quad b := 1000$$

$$f_{ck} := 30MPa \quad f_{yk} := \frac{500}{1.15} MPa$$

$$K := \frac{M}{(b \cdot d^2 \cdot f_{ck})} = 0.014$$

$$Z := d \cdot \left[ 0.5 + \left( 0.25 - \frac{K}{1.133} \right)^{0.5} \right] = 293.3 mm$$

$$\frac{Z}{d} = 0.988 \quad \text{Design for 0.95} \quad Z := 0.95 \cdot d$$

$$A_s := \frac{M}{0.87 \cdot f_{yk} \cdot Z} = 344.038 \frac{s^2 \cdot mm^2}{kg \cdot m}$$

### H14 @275 (560 mm<sup>2</sup>)

### MOMENT AT MIDSPAN LONG SPAN

$$M := \beta_{ym} \cdot n \cdot l_x^2 = 27.742 \cdot kN \cdot m \quad b := 1000$$

$$f_{ck} := 35MPa \quad f_{yk} := \frac{500}{1.15} MPa$$

$$K := \frac{M}{(b \cdot d^2 \cdot f_{ck})} = 8.986 \times 10^{-3}$$

$$Z := d \cdot \left[ 0.5 + \left( 0.25 - \frac{K}{1.133} \right)^{0.5} \right] = 294 mm$$

$$\frac{Z}{d} = 0.992 \quad \text{Design for 0.95} \quad Z := 0.95 \cdot d$$

$$A_s := \frac{M}{0.87 \cdot f_{yk} \cdot Z} = 259.94 \frac{mm^2}{m}$$

### H10 @225 (349 mm<sup>2</sup>)



## SHEAR

Coefficient (Table 3.15 BS8110)  $\beta_{vx} := 0.5$

$$V_{sx} := \beta_{vx} \cdot n \cdot l_x = 62.766 \cdot \frac{kN}{m}$$

$$v := \frac{V_{sx}}{b \cdot d} = 0.211 \cdot \frac{N}{mm^2}$$

$$v_c := \frac{100 A_s}{b \cdot d} = 0.088$$

$v < v_c$  No shear reinforcement needed

## DEFLECTION

Initial data :  $b := 1000$   $f_{yk} := 475 MPa$   $f_y := 500$   
 $f_{ck} := 35 MPa$   $d = 297$

Maximum sagging moment:

$$M_{sag} := \beta_{xe} \cdot n \cdot l_x^2 = 70.988 m^2 \cdot \frac{kN}{m}$$

$$K := \frac{M_{sag}}{(b \cdot d^2 \cdot f_{ck})} = 0.012$$

$$Z := d \cdot \left[ 0.5 + \left( 0.25 - \frac{K}{1.133} \right)^{0.5} \right] = 293 \text{ mm}$$

$$\frac{Z}{d} = 0.989 \quad \text{Design for } 0.95 \quad Z := 0.95 \cdot d$$

Reinforcement required:

$$A_s := \frac{M_{sag}}{0.87 \cdot f_{yk} \cdot Z} = 608.824 m \cdot mm^2$$

Try:  $A_{s\_eff} := 753 mm^2$  H12 @150

Actual span/depth:  $\frac{l_x}{d} = 21.886$

$$f_s := \frac{2 \cdot f_y \cdot A_s}{3 \cdot A_{s\_eff}} = 269.51 m \quad \frac{M_{sag}}{b \cdot d^2} = 0.805 m$$

Modification factor: (Table C7 in Brooker 2006)  
 $MF := 1.37$

Allowable span/depth  $MF \cdot 26 = 35.62$

$$\frac{l_x}{d} = 21.886$$

greater than  $l_x/d$  therefore ok

## 4.4 Beam analysis level 2

### BEAM REINFORCEMENT E2-F4

The irregular shape of the slab is approximated to a rectangular one of:

Dimensions:  $l_x := 6.5 m$   $l_y := 12.2 m$

$$h_{sl} := \frac{l_y}{36} = 0.339 m \quad \frac{l_y}{l_x} = 1.877$$

Effective depth:

$$h_{sl} := 350 mm \quad h_{beam} := 600 mm$$

$$f_{ck} := 30 \frac{N}{mm^2} \quad f_{yk} := 500 MPa$$

$$d := h_{beam} - 40 mm - 32 mm = 0.528 m \quad b := 400 mm$$

### ULTIMATE LOAD

Imposed load

$$g_k := h_{sl} \cdot 25 \frac{kN}{m^3} = 8.75 \cdot \frac{kN}{m^2} \quad q_k := 2.5 \frac{kN}{m^2}$$

$$\text{Ultimate load/m}^2: n := 1.35 \cdot g_k + 1.5 \cdot q_k = 15.563 \cdot \frac{kN}{m^2}$$

$$\text{Ultimate load: } UDL := n \cdot l_x \cdot l_y \cdot 0.25 = 308.527 \cdot kN$$

### Reinforcement required at support:

$$M_{sup} := UDL \cdot \frac{l_y}{12} = 313.669 \cdot kN \cdot m$$

$$K := \frac{M_{sup}}{b \cdot d^2 \cdot f_{ck}} = 0.094 \quad \text{below } 0.167, \text{ no compression reinforcement required}$$

$$Z := d \cdot \left[ 0.5 + \left( 0.25 - \frac{K}{1.133} \right)^{0.5} \right] = 479.929 \cdot mm$$

$$\frac{Z}{d} = 0.909 \quad \text{OK, above } 0.82$$

$$A_s := \frac{M_{sup}}{0.87 \cdot f_{yk} \cdot Z} = 1.502 \times 10^3 \cdot mm^2$$

$$\rho := \frac{A_s}{b \cdot d} = 0.711 \% \quad \text{Acceptable}$$

Try 3 H26 (1590 mm<sup>2</sup>)  $A_{s\_eff} := 1590 mm^2$

$$\text{Spacing } 250 - 2 \cdot 40 - 2 \cdot 10 - 26 = 124 \text{ mm}$$

Steel stress under quasi permanent loading:

$$\sigma_z := \frac{f_{yk}}{\gamma_{ms}} \left( \frac{\psi_2 \cdot q_k + g_k}{1.5 q_k + 1.35 g_k} \right) \cdot \left( \frac{A_s}{A_{s\_eff}} \right) \cdot \frac{1}{\delta} = 252.998 \cdot MPa$$

Maximum diameter 16mm or distance 175mm.  
 H28@122 acceptable.

## Reinforcement in the span

$$M_{span} := UDL \cdot \frac{l_y}{24} = 156.834 \text{ m} \cdot \text{kN}$$

$$K := \frac{M_{span}}{b \cdot d^2 \cdot f_{ck}} = 0.047 \quad \text{below } 0.167, \text{ no compression reinforcement required}$$

$$Z := d \cdot \left[ 0.5 + \left( 0.25 - \frac{K}{1.133} \right)^{0.5} \right] = 505.165 \text{ mm}$$

$$\frac{Z}{d} = 0.957 \quad \text{OK, above } 0.82$$

$$A_s := \frac{M_{sup}}{0.87 \cdot f_{yk} \cdot Z} = 1.427 \times 10^3 \cdot \text{mm}^2$$

$$\rho := \frac{A_s}{b \cdot d} = 0.676\% \quad \text{Acceptable}$$

$$\text{Try 3 H26 (1590 mm}^2) \quad A_{s\_eff} := 1590 \text{ mm}^2$$

$$\text{Spacing } 250 - 2 \cdot 40 - 2 \cdot 10 - 26 = 124 \quad \text{mm}$$

Steel stress under quasi permanent loading:

$$\sigma_z := \frac{f_{yk}}{\gamma_{ms}} \left( \frac{\psi_2 \cdot q_k + g_k}{1.5q_k + 1.35g_k} \right) \cdot \left( \frac{A_s}{A_{s\_eff}} \right) \cdot \frac{1}{\delta} = 240.359 \cdot \text{MPa}$$

Maximum diameter 16mm or distance 200mm.  
H28@122 acceptable.

## Deflection

$$\text{Reinforcement required } A_s := 1387 \text{ mm}^2$$

$$\text{Reinforcement provided } A_{s\_eff} := 2410 \text{ mm}^2$$

$$\text{Reinforcement ratio } \rho := \frac{A_s}{h_{beam} \cdot h_{sl}} = 0.66\%$$

Length to span ratio from Table NA.5, with  $f_{ck}=30$  and considering this beam as end span of a continuous beam:

$$K := 1.3$$

$$\text{From table (Mosley Fig 6.3), ratio } R := 21.7$$

$$\text{Final ratio } R := K \cdot R = 28.21$$

$$\text{To avoid damages beyond 7m: } R := R \cdot \frac{7m}{l_y} = 16.186$$

Modification for steel area provided:

$$R := R \cdot \frac{f_{yk}}{500 \text{ MPa}} \cdot \frac{A_{s\_eff}}{A_s} = 28.124$$

Span to effective depth provided:

$$\frac{l_y}{d} = 23.106 \quad \text{deflection requirements likely to be satisfied}$$

**Revise reinforcement at mid span as:  
3H32 (2410mm<sup>2</sup>) due to deflection.**

**Spacing <200 is acceptable to avoid cracking  
above 0.3mm**

## Shear

$$V_{Ed} := 145 \text{ kN}$$

$$v_{Ed} := \frac{V_{Ed}}{h_{sl} \cdot h_{beam}} = 0.69 \cdot \text{MPa}$$

$v_{Rd}$  maximum considering cotangent as 2.5 and  $f_{yk}$  as 30 MPa is:

$$v_{Rd} := 3.64 \text{ MPa}$$

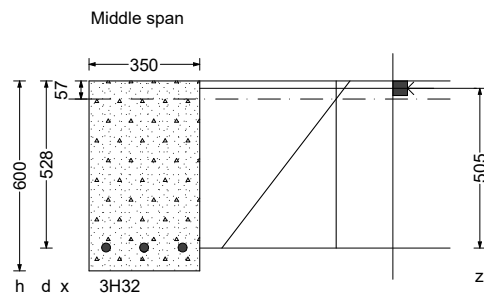
Max shear capacity greater than shear at support.

Shear reinforcement above:

$$\cot\theta := 2.5 \quad f_{ywd} := 435$$

$$\text{Reinforcement area / spacing ratio (EN1992-1-1 6.2.3(3)) } \frac{V_{Ed} \cdot 10^3}{Z \cdot f_{ywd} \cdot \cot\theta} = 0.264$$

Use H8 at 250mm



Strain diagram for the beam on level 2 at mid span

## 4.5 Column (F4) analysis level 2

Column F4 on level 2 can be analysed under the following stress:

Axial load from upper structure:

$$N_{Ed} = 4.7 \cdot 10^3 \text{ kN}$$

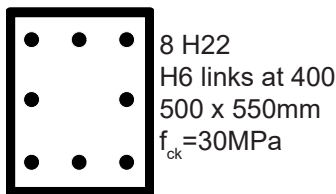
Crushing load  $N_{ult} = 5.5 \cdot 10^3 \text{ kN}$

Moment on Y direction: the moment from the beam E2-F4 is in almost equilibrium ( $M=5\text{kNm}$ ) with the moment from the slab F4-F5. The total moment is therefore:

$$M_{Edyy} = 37\text{kNm}$$

Moment on Z direction is the sum of moment produced by the flat slab (120kNm), 0.05% of moment from lateral load and the eccentricity of the axial load.

$$M_{Edzz} = 108\text{kNm}$$



Summary for column F4

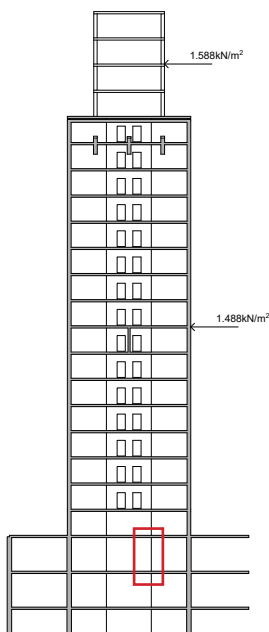


Figure 4.5.1: diagram showing the wind loading acting on the building

**COLUMN** Level 2 Column F4

### DIMENSIONS AND MATERIAL CHARACTERISTICS

Column

$$y := 500\text{mm} \quad z := 550\text{mm} \quad h_{col} := 3.5\text{m}$$

$$dia_{bar} := 22\text{mm} \quad dia_{link} := 8\text{mm}$$

$$f_{cd} := \frac{30}{1.5} \text{MPa} \quad f_{yd} := \frac{500}{1.5} \text{MPa}$$

Beam E2-F4

$$y_{24} := 12.2\text{m} \quad z_{24} := .35\text{m} \quad h_b := .55\text{m}$$

Slab Grid 5-6

$$y_{45} := 7.5\text{m} \quad z_{45} := 5.1\text{m} \quad h_{slab} := .30\text{m}$$

### COVER

As per EN1992-1-2 Table 5.2a and REI120 45mm  
 $cover := 45\text{mm}$

### ACTIONS

Load from slab weight, variable load and cladding.  
Y direction grid 2-4, Z direction grid E to F

Equation 6.10 is used, with factor obtained from National Annex of:

Permanent actions unfavourable:  $\gamma_{pu} := 1.35$

Permanent actions favourable:  $\gamma_{pf} := 1$

Leading variable actions unfavourable:  $\gamma_{vu} := 1.5$

Leading variable actions favourable:  $\gamma_{vf} := 0$

Leading variable actions unfavourable:  $\gamma_{au} := 1.5 \cdot 0.7$

Accompanying variable actions favourable:  $\gamma_{af} := 0$

### AXIAL LOADING

$$g_k := 25 \frac{\text{kN}}{\text{m}^3} \cdot h_{\text{slab}} = 7.5 \cdot \frac{\text{kN}}{\text{m}^2} \quad g_{\text{clad}} := 2 \frac{\text{kN}}{\text{m}^2}$$

$$q_k := 2.5 \frac{\text{kN}}{\text{m}^2} = 2.5 \cdot \frac{\text{kN}}{\text{m}^2}$$

Area supported on levels 18-22:

$$A_{1922} := 4\text{m} \cdot 5.3\text{m} = 21.2\text{m}^2$$

Sum of Area supported on levels 3-18:

$$A_{318} := 102\text{m}^2$$

### Permanent loading:

$$G_{1922} := A_{1922} \cdot (\gamma_{pu} \cdot g_k) \cdot 4 = 858.6 \cdot \text{kN}$$

$$G_{318} := A_{318} \cdot (\gamma_{pu} \cdot g_k) = 1.033 \times 10^3 \cdot \text{kN}$$

For cladding

$$G_{1922c} := \left( 7\text{m} \cdot 3.5\text{m} \cdot 2 \frac{\text{kN}}{\text{m}^2} \right) \cdot 4 \cdot \gamma_{pu} = 264.6 \cdot \text{kN}$$

$$G_{318c} := \gamma_{pu} \left( 3.75\text{m} \cdot 3.5\text{m} \cdot 15 \dots + 3.5\text{m} \cdot 15 \cdot \frac{12\text{m}}{2} \right) \cdot 2 \frac{\text{kN}}{\text{m}^2} = 1.382 \times 10^3 \cdot \text{kN}$$

Columns :

$$G_{1922cl} := \gamma_{pu} \cdot 3.5\text{m} \cdot 4 \cdot 35\text{m} \cdot 45\text{m} \cdot 25 \frac{\text{kN}}{\text{m}^3} = 74.419 \cdot \text{kN}$$

$$G_{318cl} := \gamma_{pu} \cdot 3.5\text{m} \cdot 15 \cdot 45\text{m} \cdot 55\text{m} \cdot 25 \frac{\text{kN}}{\text{m}^3} = 438.539 \cdot \text{kN}$$

$$G_{\text{tot}} := G_{1922} + G_{318} + G_{1922c} \dots = 4.051 \times 10^6 \text{ N} \\ + G_{318c} \dots \\ + G_{1922cl} + G_{318cl}$$

Q <sub>k</sub> 7kN/m		Q <sub>k</sub> 19 kN/m
G <sub>k</sub> 15 kN/m	G <sub>k</sub> 51 kN/m	G <sub>k</sub> 51 kN/m
11.2m	7.5m	7.5m

Figure 4.5.2 load distribution along E2-F4-F7 on level 2

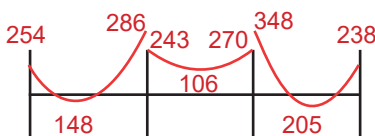


Figure 4.5.3: moment distribution along E2-F4-F7 on level 2

### Leading variable action:

The leading variable is assumed to be variable loads on the structure. Wind is considered accompanying variable due to shear walls taking most of lateral force and leaving each column with 0.05% of the load.

$$Q_{1922} := A_{1922} \cdot (\gamma_{vu} \cdot q_k) \cdot 4 = 318 \cdot \text{kN}$$

$$Q_{318} := A_{318} \cdot (\gamma_{vu} \cdot q_k) = 382.5 \cdot \text{kN}$$

$$Q_{\text{tot}} := Q_{1922} + Q_{318} = 7.005 \times 10^5 \text{ N}$$

$$N_{Ed} := Q_{\text{tot}} + G_{\text{tot}} = 4.751 \times 10^3 \cdot \text{kN}$$

### Accompanying variable (wind)

Wind pressure is simplified as:

$$\text{Levels 19-22} \quad P_{1922} := 1.588 \frac{\text{kN}}{\text{m}^2}$$

$$\text{Levels 19-22} \quad P_{318} := 1.488 \frac{\text{kN}}{\text{m}^2}$$

The application point in respect to the column base on level 2 is placed halfway through the height section considered:

$$L_{1922} := 72.6\text{m} - 9.6\text{m} = 63\text{m}$$

$$L_{318} := 37.7\text{m} - 9.6\text{m} = 28.1\text{m}$$

Facade area:

$$A_{1922} := 14\text{m} \cdot 19.8\text{m} = 277.2\text{m}^2$$

$$A_{318} := 1447\text{m}^2$$

Force applied in each section of the building:

$$F_{w1922} := A_{1922} \cdot P_{1922} = 4.402 \times 10^5 \text{ N}$$

$$F_{w318} := A_{318} \cdot P_{318} = 2.153 \times 10^6 \text{ N}$$

Portion (0.05%) of the moment produced at the base of the column by wind:

$$M_W := \left( F_{w1922} \cdot L_{1922} \dots + F_{w318} \cdot L_{318} \right) \cdot 0.05\% = 44.118 \cdot \text{kN} \cdot \text{m}$$

## DISTRIBUTION FACTORS

Stiffness, upper column  $E_{uc} := \frac{y^3 \cdot z}{h_{col}} = 19.643 L$

Stiffness, lower column  $E_{lc} := E_{uc}$

Stiffness, beam E2-F4

$$E_{b24} := z_{24} \cdot \frac{h_b^3}{y_{24}} = 4.773 L$$

Stiffness, slab grid 45,

$$E_{sl45} := z_{45} \cdot \frac{h_{slab}^3}{y_{45}} = 18.36 L$$

Distribution factor upper and lower column in F4

$$DF_{uc} := \frac{E_{uc}}{E_{lc} + E_{uc} + E_{b24} + E_{sl45}} = 0.315$$

Distribution factor for beam 24

$$DF_{sl24} := \frac{E_{b24}}{E_{lc} + E_{uc} + E_{b24} + E_{sl45}} = 0.076$$

Distribution factor Y direction slab 56

$$DF_{sl45} := \frac{E_{sl45}}{E_{lc} + E_{uc} + E_{b24} + E_{sl45}} = 0.294$$

Distribution factor upper and lower column F5

$$DF_{uc} := \frac{E_{uc}}{E_{lc} + E_{uc} + E_{sl45} + E_{sl45}} = 0.258$$

Distribution factor upper and lower column F7

$$DF_{uc} := \frac{E_{uc}}{E_{lc} + E_{uc} + E_{sl45}} = 0.341$$

Distribution factor upper and lower column E2

$$DF_{uc} := \frac{E_{uc}}{E_{lc} + E_{uc} + E_{b24}} = 0.446$$



Figure 4.5.4: distribution factors along E2-F4-F7 on level 2

## SLENDerness CHECK

factor := 0.85 From BS8110:Part 1:1997

$$I_0 := (3500mm - 300mm) \cdot factor = 2.72m$$

$$\lambda_z := 3.46 \cdot \frac{I_0}{z} = 17.111 \quad \lambda_y := 3.46 \cdot \frac{I_0}{y} = 18.822$$

$$A := 0.7$$

A.s taken from end of calculation:

$$\omega := \frac{A_s \cdot f_{yd}}{y \cdot z \cdot f_{cd}} = 0.152 \quad B := (1 + 2 \cdot \omega)^{0.5} = 1.142$$

Worst case for braced structures

$$C := 1.7$$

$$n := \frac{N_{Ed}}{y \cdot z \cdot factor \cdot f_{cd}} = 1.016$$

$$\lambda_{lim} := 20 \cdot \frac{A \cdot B \cdot C}{n^{0.5}} = 26.948$$

Column not slender since  $\lambda_{lim} > \lambda_y$  and  $\lambda_z$

## LOADS FROM SLAB ON LEVEL 2

$$UDL_{24} := z_{24} \cdot (1.35 \cdot g_k + 1.5 \cdot q_k) = 4.856 \cdot \frac{kN}{m}$$

$$UDL_{45} := z_{45} \cdot (1.35 \cdot g_k + 1.5 \cdot q_k) = 70.763 \cdot \frac{kN}{m}$$

$$UDL_{45min} := z_{45} \cdot 1.5 \cdot g_k = 57.375 \cdot \frac{kN}{m}$$

$$UDL_{z24} := y_{24} \cdot (1.35 \cdot g_k + 1.5 \cdot q_k) = 169.275 \cdot \frac{kN}{m}$$

$$UDL_{z45} := y_{45} \cdot (1.35 \cdot g_k + 1.5 \cdot q_k) = 104.063 \cdot \frac{kN}{m}$$

## MOMENTS FROM STRUCTURE ON LEVEL 3

In Y direction the total moment is given by moment created by horizontal structure in level 3 and axial load:

$$M_{str.y} := 21kN \cdot m$$

$$M_{Edyy} := M_{str.y} + N_{Ed} \cdot \frac{I_0}{400} = 53.31 \cdot kN \cdot m$$

In Z direction the moment from the flat slab is limited to 120kNm since F4 is an edge column. Worst case, with wind in the same direction was considered

$$M_{str.z} := 120kN \cdot m \quad M_w = 44.118 \cdot kN \cdot m$$

$$M_{Edzz} := M_{str.z} + M_w + N_{Ed} \cdot \frac{I_0}{400} = 196.428 \cdot kN \cdot m$$

## DESIGN REINFORCEMENT

$$f_{ck} := 30 \text{ MPa}$$

$$f_{yk} := 500 \frac{\text{N}}{\text{mm}^2}$$

$$\frac{M_{Edzz}}{y \cdot z^2 \cdot f_{ck}} = 0.043$$

$$\frac{N_{Ed}}{y \cdot z \cdot f_{ck}} = 0.576$$

$$z = 0.55 \text{ m}$$

$$d_2 := \text{cover} + \text{dia}_{link} + \text{dia}_{bar} \cdot 0.5 = 0.064 \text{ m}$$

$$\frac{d_2}{z} = 0.116$$

From chart  $A_s$   $f_{yk}$  /  $b h f_{yk}$  (Harrison2007a, p39)

$$\text{ratio} := 0.11$$

$$A_s := \frac{\text{ratio} \cdot y \cdot z \cdot f_{ck}}{f_{yk}} = 1.815 \times 10^3 \cdot \text{mm}^2$$

$$8 \text{ bars H18 (2040 mm}^2) \quad A_s := 2040 \text{ mm}^2$$

Crushing load of a truly loaded column may be taken as: (Mosley, p.267)

$$N_{ud} := 0.567 \cdot f_{ck} \cdot y \cdot z + 0.87 \cdot A_s \cdot f_{yk} = 5.565 \times 10^3 \cdot \text{kN}$$

$$N_{Ed} = 4.751 \times 10^3 \cdot \text{kN}$$

Minimum area of steel needs to be above 0.002Ac

$$A_{s_{min}} := 0.002 \cdot y \cdot z = 550 \cdot \text{mm}^2 \quad \frac{A_s}{z \cdot y} = 0.742 \cdot \%$$

## DESIGN FIRE RESISTANCE

check that effective length < 3m

$$l_0 := (3.1 \text{ m} - 0.3 \text{ m}) \cdot 0.85 = 2.38 \text{ m} \quad \text{OK}$$

$$\text{check } e < e_{\text{max}} \quad e := \frac{M_{Edyy}}{N_{Ed}} = 0.011 \text{ m}$$

$$e_{\text{max}} := 0.15 \cdot z = 0.083 \text{ m} \quad \text{OK}$$

$$\text{Check reinforcement } < 4\% \quad \frac{A_s}{z \cdot y} = 0.742 \cdot \% \quad \text{OK}$$

## CHECK BIAXIAL BENDING

$$N_{Ed} = 4.751 \times 10^6 \text{ N}$$

$$e_z := \frac{M_{Edzz}}{N_{Ed}} = 41.34 \cdot \text{mm} \quad e_y := \frac{M_{Edyy}}{N_{Ed}} = 11.22 \cdot \text{mm}$$

$$\frac{e_y}{e_z} = 0.271 \quad \text{between 0.2 and 5, design for biaxial bending needs to be checked}$$

From chart obtain ratio of  $A_s$   $f_{yk}$  /  $b h f_{ck}$

Revise reinforcement to 8 H22 (3040 mm<sup>2</sup>)

$$A_{s_{eff}} := 3040 \text{ mm}^2 \quad A_{s_{eff}} \cdot \frac{f_{yk}}{y \cdot z \cdot f_{ck}} = 0.184$$

$$\frac{N_{Ed}}{z \cdot y \cdot f_{ck}} = 0.576 \quad \frac{d_2}{y} = 0.128$$

$$f_{chart} := 0.05$$

$$M_{Rd} := f_{chart} \cdot y \cdot z^2 \cdot f_{ck} = 226.875 \cdot \text{kN} \cdot \text{m}$$

$$N_{Rd} := z \cdot y \cdot f_{cd} \cdot 0.85 + A_{s_{eff}} \cdot f_{yd} = 5.688 \times 10^3 \cdot \text{kN}$$

Value for a obtained from chart (Harrison2007a, Table 5):

$$\frac{N_{Ed}}{N_{Rd}} = 0.835 \quad a := 1 + \left( \frac{N_{Ed}}{N_{Rd}} - 0.1 \right) \cdot \frac{0.5}{0.6} = 1.613$$

$$\left( \frac{M_{Edzz}}{M_{Rd}} \right)^a + \left( \frac{M_{Edyy}}{M_{Rd}} \right)^a = 0.889 \quad \text{Acceptable}$$

## CHECK REINFORCEMENT

$$A_s \text{ minimum} \quad \frac{0.10 N_{Ed}}{f_{yd}} = 1.425 \times 10^3 \cdot \text{mm}^2$$

$$\text{Reinforcement to area ratio} \quad \frac{A_{s_{eff}}}{y \cdot z} = 1.105 \cdot \%$$

Reinforcement is above 0.2% and below 4% and above  $A_s$  minimum.

## TRANSVERSE REINFORCEMENT

Ref. EC2 9.5.3&NA

Diameter of bar should exceed 6m of 1/4 of reinforcement bars

$$\text{dia}_{min} := \text{dia}_{bar} \cdot 0.25 = 5.5 \cdot \text{mm}$$

**Diameter 6mm**

Spacing given by the minimum

$$20 \cdot \text{dia}_{bar} = 440 \cdot \text{mm}$$

$$y = 500 \cdot \text{mm}$$

$$400 \text{ mm} = 400 \cdot \text{mm}$$

**H6 @ 400 mm**

$$z \cdot y \cdot f_{cd} \cdot 0.85 = 4.675 \times 10^6 \text{ N}$$

## 5. Horizontal loading, shear walls

Horizontal loading is mostly caused by wind. A preliminary analysis on the tensile stress applied to the shear wall was done in three point of the building. it was possible to have a first estimate of the amount of shear wall needed in different part of the building.

Figures 5.1, 5.2 and 5.3 show a possible layout for shear walls. As previously stated, upper levels, used as a penthouse are kept as free of vertical elements as possible. In the lower levels (2-18) partitions between apartments were assumed as shear walls. This seemed a reasonable assumption considering that the layout of the different units is unlikely to change.

A summary of result is show in Table 5.1 and calculation for one of the three levels in the following page.

Figure 5.1: structural diagram with shear walls on level 18

Level	Wall	$N_{Ed}$ (kN)	DF	"Wk (kNm)	$\sigma$ (MPa)	$A_s$ (mm <sup>2</sup> )	Reinf
17	D5	1254	49%	3397	10	7497	H25@125 x2
10	D5	1591	4%	2652	8.4	5853	H24@150 x2
2	D5	2600	4%	4230	12.2	8400	H28@125 x2

An additional source for horizontal loading is created by the slanted structure on grid 2. In Figure 5.4 shows a diagram visualizing the sub-frame on level 2. The horizontal component of the axial loading acting on the column will produce a force  $F = \text{axial loading} \cdot \cos(77^\circ)$ . This force should be considered in the analysis of the vertical structure on grid 4 especially at the point D4 where the beams meet the vertical shear wall.

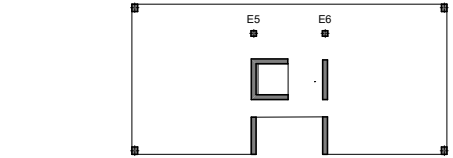


Figure 5.1: structural diagram with shear walls on level 18

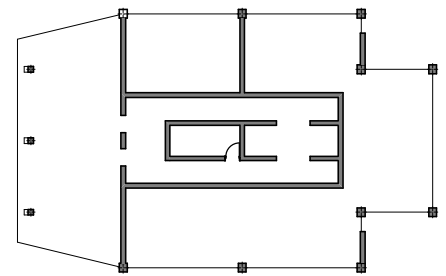


Figure 5.2: structural diagram with shear walls on level 10

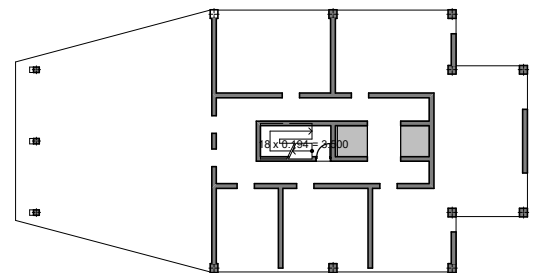


Figure 5.3: structural diagram with shear walls on level 3

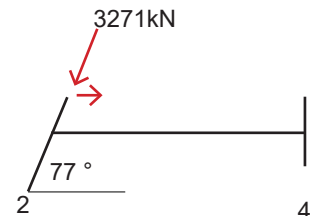


Figure 5.4: diagram showing the slanted column on

## SHEAR WALL (D5) ON LEVEL 2

### Axial load:

Tributary area on supported by the wall  $A := 8m^2$

$$\text{Load per m}^2 \quad g_k := 7.5 \frac{kN}{m^3} \cdot .3m = 2.25 \times 10^3 Pa$$

Floors := 20

Wal dimensions  $t := 0.3m$   $L := 2.5m$

Load from wall:

$$g_{wall} := L \cdot t \cdot 3.5m \cdot \text{Floors} \cdot 25 \frac{kN}{m^3} = 1.313 \times 10^3 \cdot kN$$

Load from variable load:

$$q_k := 5 \frac{kN}{m^2} \cdot A \cdot \text{Floors} = 800 \cdot kN$$

Permanent actions unfavourable:  $\gamma_{pu} := 1.35$

Leading variable actions unfavourable:  $\gamma_{vu} := 1.5$

Accompanying variable actions unfavourable:  $\gamma_{au} := 1.5 \cdot 0.7$

$$N_{Ed} := (g_{wall} + A \cdot g_k) \cdot \gamma_{pu} \dots = 2.636 \times 10^3 \cdot kN \\ + \gamma_{au} \cdot q_k$$

### Moment generated by wind action:

Upper part, levels 18-22

$$P := 1.588 \frac{kN}{m^2}$$

$$A_w := 4 \cdot 3.5m \cdot 19.8m = 277.2m^2$$

$L_{wind} := 68m$

$$W_{k1} := P \cdot A_w \cdot L_{wind} = 2.993 \times 10^4 \cdot kN \cdot m$$

Lower part, levels 2-18

$$P := 1.588 \frac{kN}{m^2}$$

$$A_w := 1415m^2$$

$L_{wind} := 31.5m$

$$W_{k2} := P \cdot A_w \cdot L_{wind} = 7.078 \times 10^4 \cdot kN \cdot m$$

$$W_{k\_tot} := W_{k1} + W_{k2} = 1.007 \times 10^5 \cdot kN \cdot m$$

Moment acting on the column:

Portion of moment take  $f := .028$

$$W_k := W_{k\_tot} \cdot f = 2.82 \times 10^3 \cdot kN \cdot m$$

## SHEAR WALLS

Ultimate axial load  $N_{Ed} = 2.636 \times 10^3 \cdot kN$

Ultimate in-plane moment  $W_k = 2.82 \times 10^3 \cdot kN \cdot m$

Length of the wall  $L := 2.5m$

Thickness of the wall  $t_{wall} := .3m$

Maximum applied tensile stress:

$$M := W_k \cdot \gamma_{vu} = 4.23 \times 10^3 \cdot kN \cdot m$$

$$\sigma := \frac{N}{L \cdot t} + \frac{M}{\left( \frac{t_{wall} \cdot L^2}{6} \right)} = 13.536 \cdot MPa$$

Area of reinforcement required:

Length of wall in tension  $L_t := 1m$

$f_y := 500MPa$

$$A_{min} := \frac{\sigma \cdot L_t \cdot t_{wall}}{0.87 \cdot f_y} = 9.335 \times 10^3 \cdot mm^2$$

### H28 @125 (4928 mm<sup>2</sup>) on both face of the wall

Ultimate compressive load should be less than:

Area of concrete per unit length of wall  $A_c := 1m \cdot t = 3 \times 10^5 \cdot mm^2$

$f_{cu} := 30MPa$

$$F_c := 0.35f_{cu} \cdot A_c + 0.67f_y \cdot A_{min} = 6.277 \times 10^3 \cdot kN$$



## 6. Health and Safety

The CDM 2015 regulation requires the designer to (amongst other duties):

- avoid foreseeable risks
- provide adequate information about significant risk
- co-ordinate their work with others

At the moment, being at a conceptual level of the design and with scarce site information, it becomes difficult to describe specific solutions. The main activities that would be carried are therefore described.

The first obligation, regarding the reduction of risks, can be addressed during different phases of the project. During pre-construction phase, together with client, gather available information related to health. Sources may be previous health and safety files, local conditions and regulations, assessment of the site. Fill gaps and provide information to designer and contractors. The preparation of a Construction Method Statement and a Construction Phase Plan (by principal contractor) will help in better understanding the construction process and related risks. These documents will inform on possible site rules and arrangements and requirements (CDM2015, Schedule 2) to be taken to ensure safety.

During the design phase, evaluate and foresee if particular details or moments during the construction may cause a hazard to workers. Possible hazards may be created by the movement of heavy pieces, use of dangerous tools, working at height, handling hazardous materials (see also CDM 2015, Schedule 3). Consider possible solutions by assessing alternatives and applying the general principles of preventions (CDM2015, Appendix ).

The main document to provide information on risk is the Health and Safety File (CDM 2015, Appendix 4). This document shall be prepared by the principal designer. Feedback and coordination with client and contractors is essential.

The third obligation, to be fulfilled, requires the creation of a health and safety file. It is essential to involve client and contractors in the process and to make sure workers are aware of its content. It is important to establish a line of communication across client, designers, contractors and workers. It may be noted that a project of this size will involve numerous contractors and many of them will join the project at a later stage. The transmission of information should also consider this. Additionally, the file should be thought as a "live document" that can be updated and adjusted during the process. Feedback from workers is essential therefore a system supporting it should be created.

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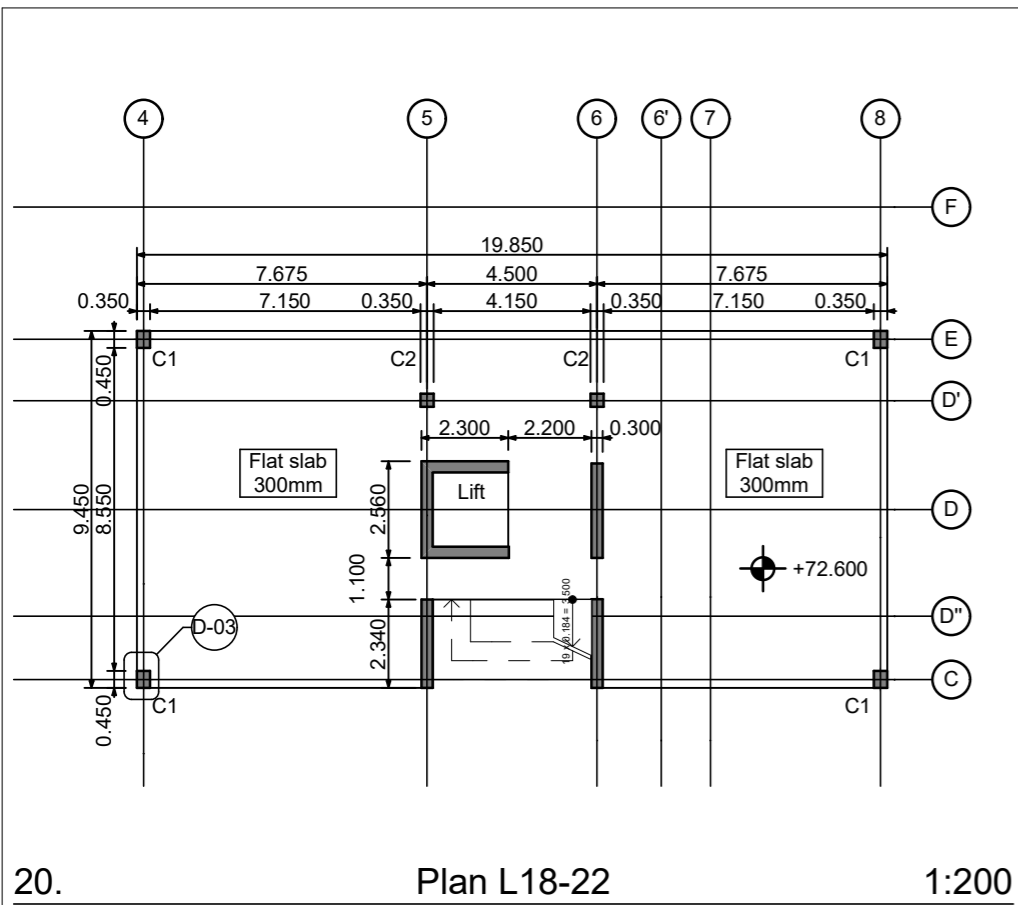
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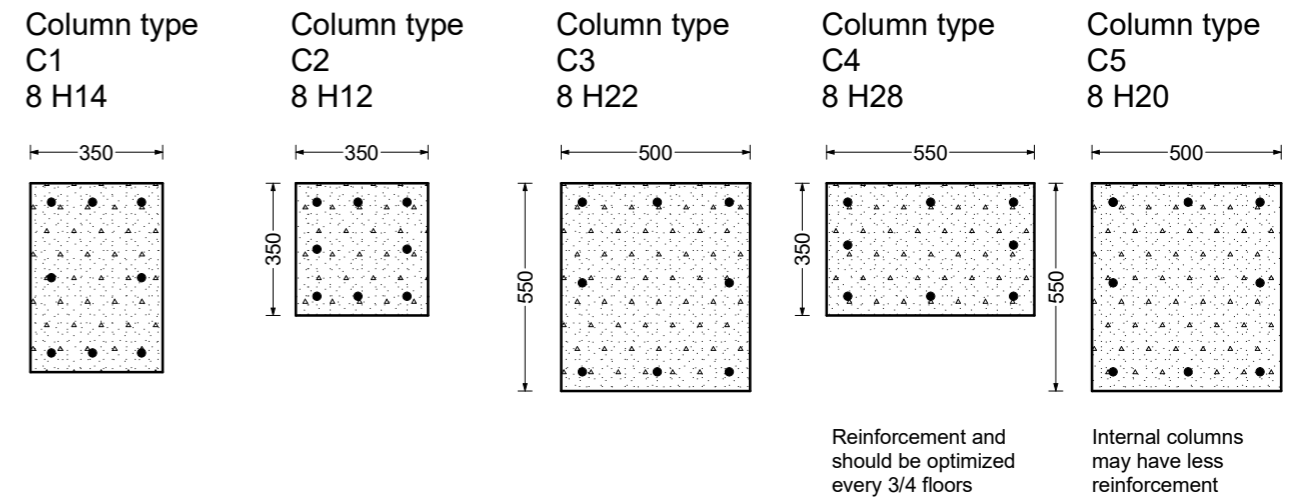
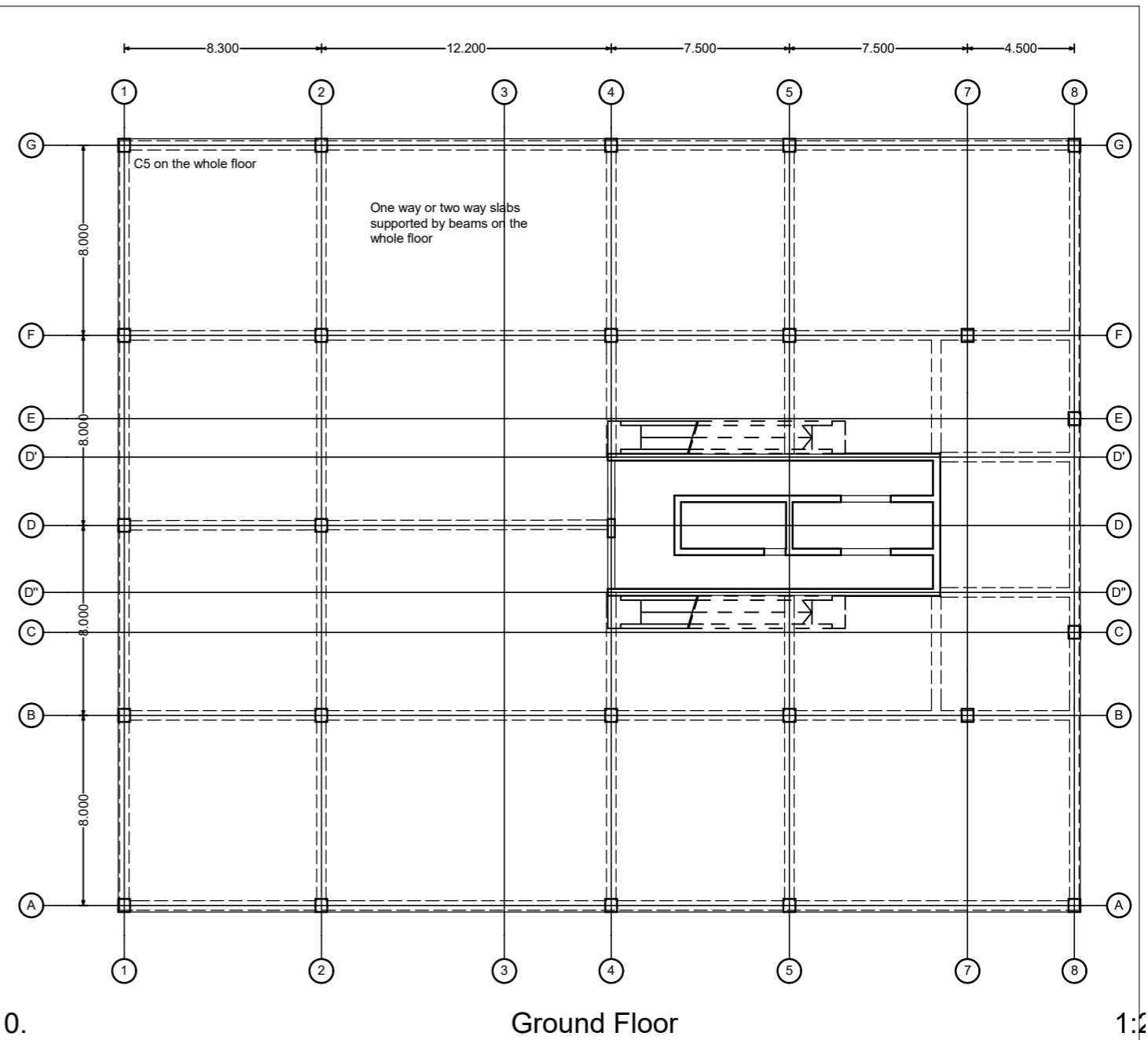
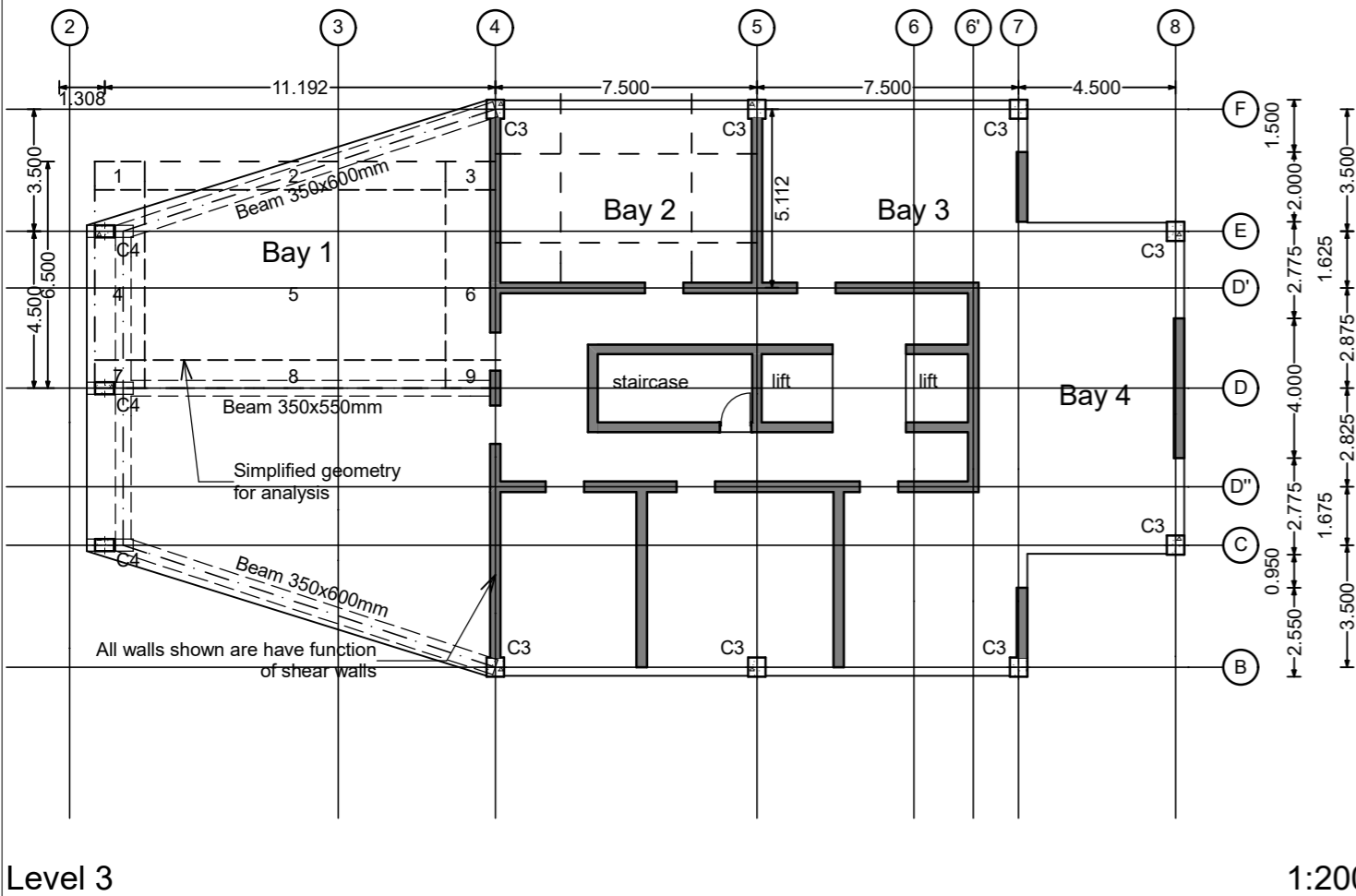
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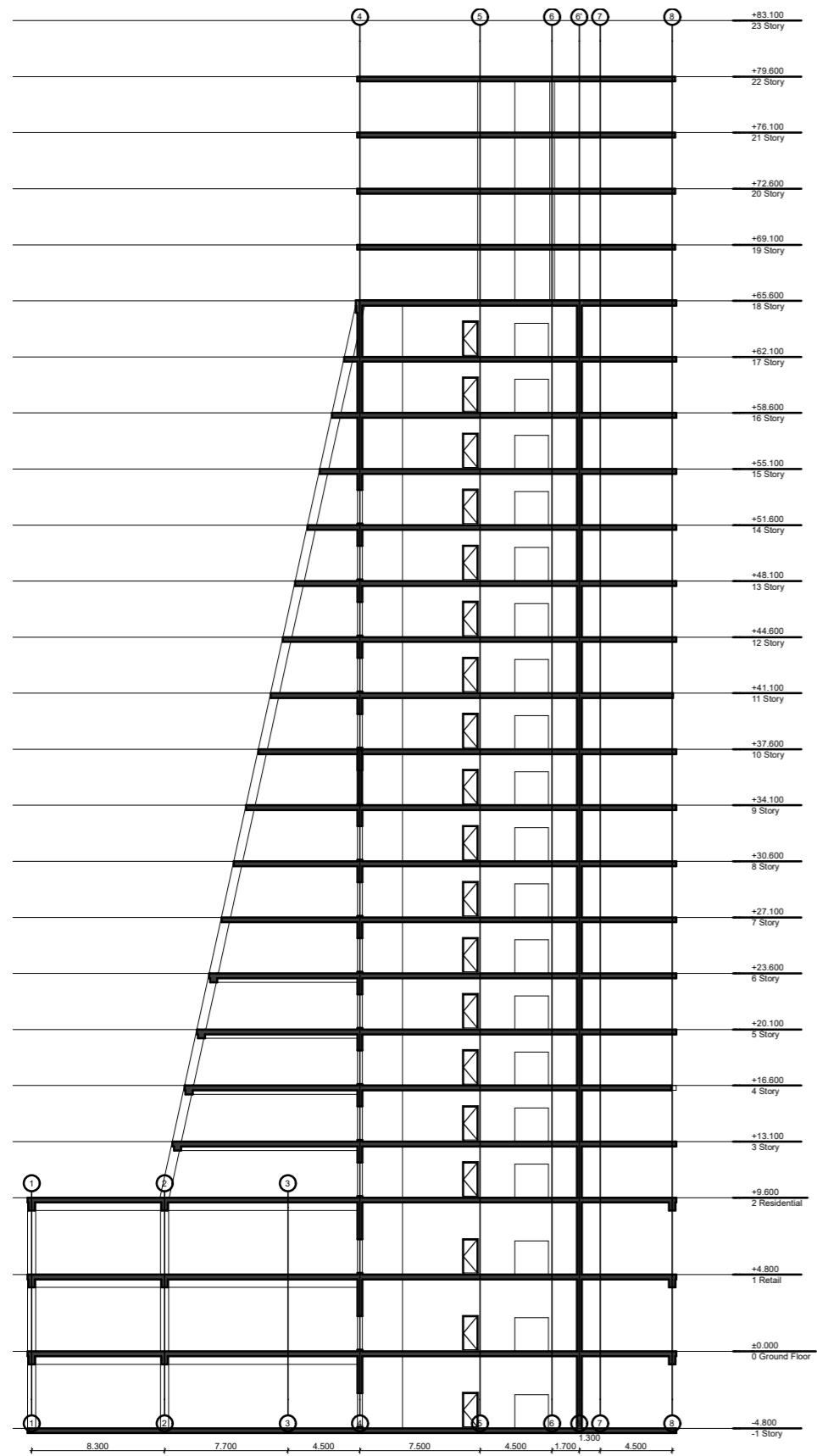


Note: the analysis for Bay 2 was simplified: a support at each of the four corners was assumed

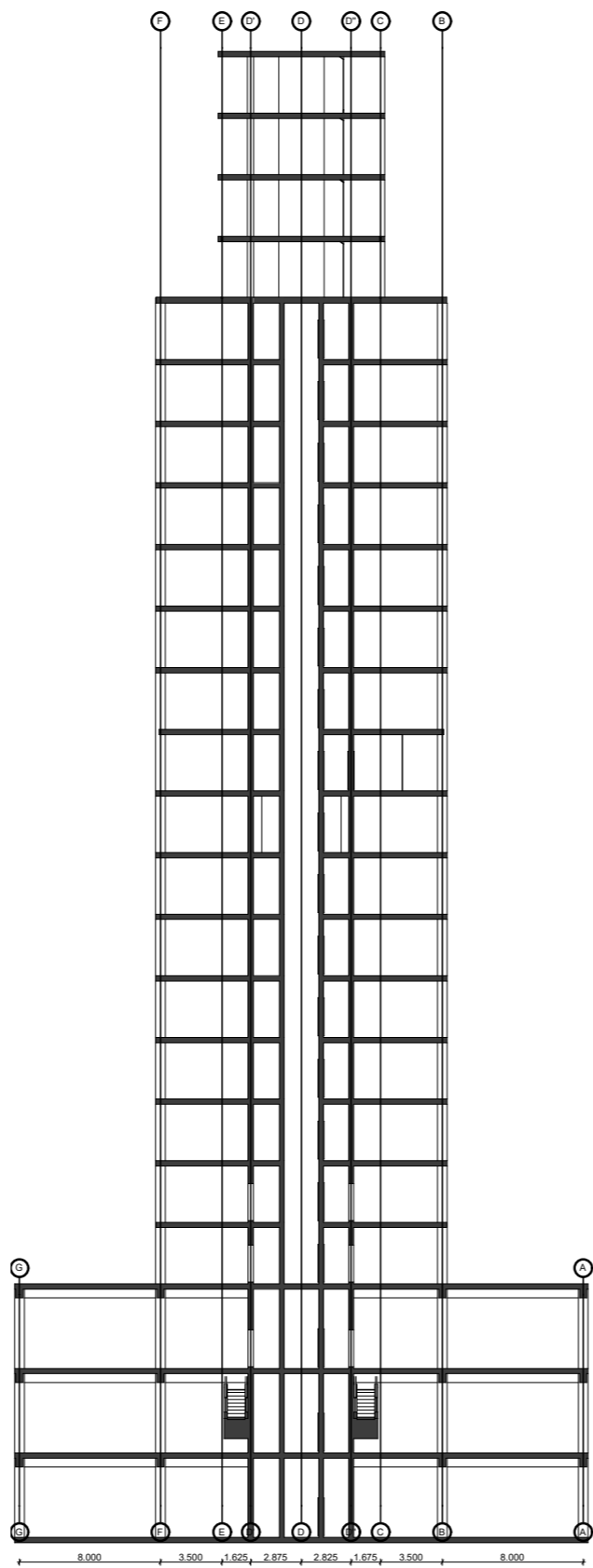


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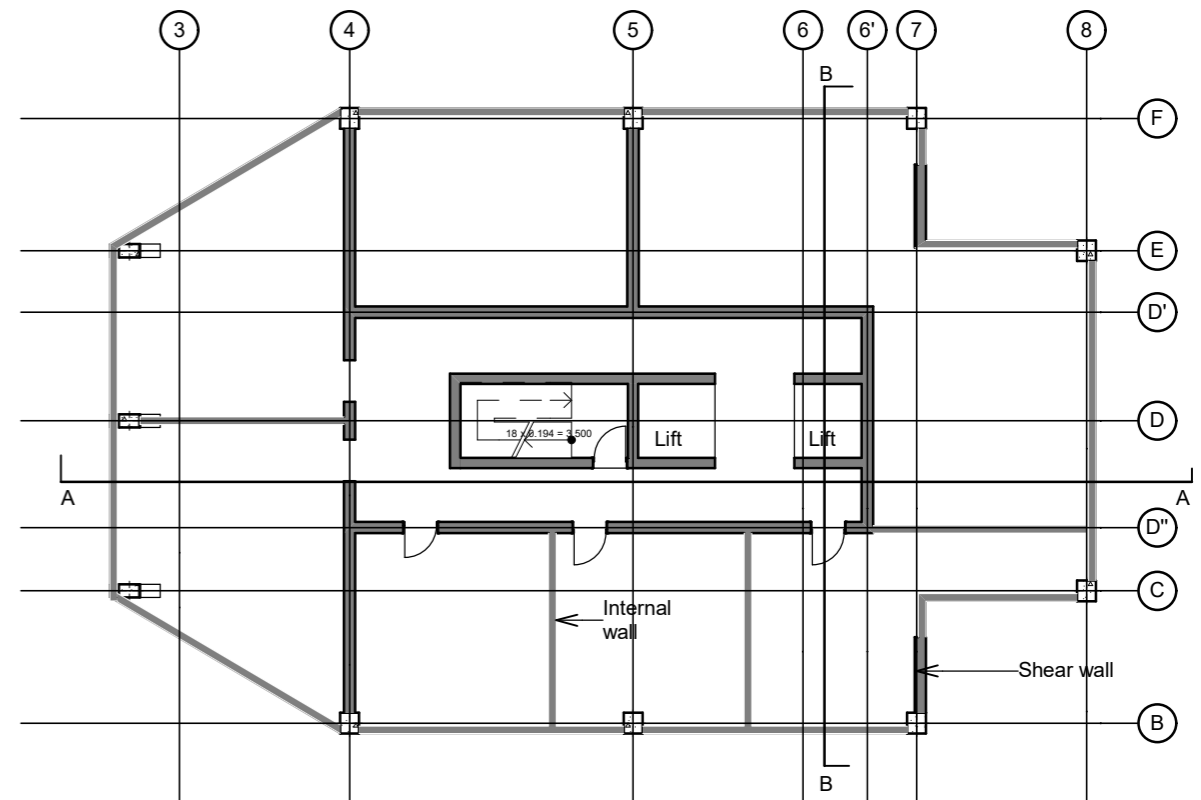
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Structural plans



AA Building Section 1:400



BB Building Section 1:400



10. Layout 1:200

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